



**INTERNATIONAL POTATO CENTER  
1971 - 2011**



version 1.1-2

## **PRACTICAL MANUAL**

**Felipe de Mendiburu  
RESEARCH INFORMATIC UNIT**

**July - 2012**

---

## INDEX

	Page
PREFACE	1
1. INSTALLATION OF AGRICOLAE AND USE IN R	1
1.1 INSTALLATION	1
1.2 USE IN R	2
2. DESCRIPTIVE STATISTICS	3
2.1 HISTOGRAM	3
2.2 HANDLING SCALES	4
2.3 FREQUENCY TABLES AND STATISTICS	5
2.4 REPRODUCING HISTOGRAMS AND USE OF hist()	5
2.5 HISTOGRAM BASED ON GROUPED DATA	6
2.6 JOINING CLASSES	7
3. EXPERIMENT DESIGNS	7
3.1 COMPLETELY RANDOMIZED DESIGNS	7
3.2 RANDOMIZED COMPLETE BLOCK DESIGN	8
3.3 LATIN SQUARE DESIGNS	8
3.4 GRAECO-LATIN DESIGNS	8
3.5 BALANCED INCOMPLETE BLOCK DESIGNS	8
3.6 CYCLIC DESIGNS	9
3.7 LATTICE DESIGNS	10
3.8 ALPHA DESIGNS	10
3.9 AUGMENTED BLOCK DESIGNS	11
3.10 SPLIT-PLOT DESIGNS	12
3.11 STRIP-PLOT DESIGNS	12

4. MULTIPLE COMPARISONS	13
4.1 THE LEAST SIGNIFICANT DIFFERENCE (LSD)	14
4.2 BONFERRONI	15
4.3 DUNCAN'S NEW MULTIPLE-RANGE TEST	16
4.4 STUDENT-NEWMAN-KEULS	17
4.5 TUKEY'S W PROCEDURE (HSD)	18
4.6 WALLER-DUNCAN'S BAYESIAN K-RATIO t-TEST	18
4.7 SCHEFFE'S TEST	20
4.8 GRAPHICS OF THE MULTIPLE COMPARISON	21
4.9 ANALYSIS OF BALANCED INCOMPLETE BLOCKS	22
4.10 PARTIALLY BALANCED INCOMPLETE BLOCKS	24
4.11 AUGMENTED BLOCKS	30
4.12 NON-PARAMETRIC COMPARISONS	33
4.13 KRUSKAL-WALLIS	33
4.14 FRIEDMAN	34
4.15 WAERDEN	35
4.16 DURBIN	36
5. STABILITY ANALYSIS	37
5.1 PARAMETRIC STABILITY	37
5.2 NON-PARAMETRIC STABILITY	39
5.3 AMMI	41
6. SPECIAL FUNCTIONS	42
6.1 CONSENSUS OF DENDROGRAM	42
6.2 MONTECARLO	44
6.3 RE-SAMPLING IN LINEAR MODEL	46
6.4 SIMULATION IN LINEAR MODEL	46
6.5 PATH ANALYSIS	47
6.6 LINE X TESTER	48
6.7 SOIL UNIFORMITY	50
6.8 CONFIDENCE LIMITS IN BIODIVERSITY INDICES	51
6.9 CORRELATION	52
6.10 OTHER FUNCTIONS	53
REFERENCES	57

## PREFACE

R is a functional programming system exclusive to manage data in statistics and related sciences, such as mathematics, in environments like Windows, Linux and MAC. 'Agricolae' is a package of functions for R applied to agricultural research.

The package 'agricolae' offers a broad functionality in the design of experiments, especially for experiments in agriculture and improvements of plants, which can also be used for other purposes. It contains the following designs: lattice, alpha, cyclic, balanced incomplete block designs, complete randomized blocks, Latin, Graeco-Latin, augmented block designs, divided parcels, divided blocks. It also has several procedures of experimental data analysis, such as the comparisons of treatments of Waller-Duncan, Bonferroni, Duncan, Student-Newman-Keuls, Scheffe, or the classic LSD and Tukey; and non-parametric comparisons, such as Kruskal-Wallis, Friedman, Durbin and Waerden, stability analysis, and other procedures applied in genetics, as well as procedures in biodiversity and descriptive statistics.

For more details on the use of 'agricolae', see the reference manual and the aid system in HTML, which can be found in the menu of R.

## 1 INSTALLATION OF AGRICOLAE AND USE IN R

### 1.1 INSTALLATION

The main program of R should be already installed in the platform of your computer (Windows, Linux or MAC). If it is not installed yet, you can download it from the R project ([www.r-project.org](http://www.r-project.org)) of a repository CRAN (R Development Core Team, 2012). As it is a free program, no identification is required. The packages can be incorporated through an installation process, directly from the platform of R.

'Agricolae' is a package for R, and as such its installation is just like any other package of R.

For Windows, the R program (version 2.15.1 or higher) is required.

If the R program is already installed in Windows or in another platform, the installation of 'agricolae' can be done directly from the console of R through Internet, that is

```
install.packages("agricolae")
```

A repository should be selected and the system is installed automatically.

If there is no Internet connection, it is necessary to copy the file agricolae\_1.1-2. zip for Windows from the page of the R project.

The file agricolae\_1.1-2.zip (De Mendiburu, 2012) can be downloaded from the R repository in the following addresses: [www.r-project.org](http://www.r-project.org) or <http://cran.at.r-project.org/web/packages/agricolae/index.html>

The file can be directly incorporated into R installing from the console with the following instruction set if the file is located in the address E:  
`install.packages("E:/agricolae_1.1-2.zip")`

It can also be installed from the R menu:

Packages, Install package(s) from local zip files.... Selecting the file zip does not require any unpacking.

For a complete functionality, 'agricolae' requires other packages.

MASS: for the generalized inverse used in the function `PBIB.test()`

klaR: for the function `triplot()` used in the function `AMMI()`

akima: for the use of the function `interp()` used in `grid3p()` for interpolation

Cluster: for the use of the function `consensus()`

## 1.2 USE IN R

Since 'agricolae' is a package of functions, these are operational when they are called directly from the console of R and are integrated to all the base functions of R.

The following orders are frequent:

Load the package to the memory: `library(agricolae)`

Download: `detach(package:agricolae)`

Once the package is loaded, you can:

List the database: `data(package="agricolae")`

Load the sweet potato data: `data(sweetpotato)`

See its structure: `str(sweetpotato)`

Publish its content: `fix(sweetpotato)`

In order to continue with the command line, do not forget to close the open windows with any R order.

For help: `help(sweetpotato)`; `? sweetpotato`

To search any functions: `apropos("design")`

[1] "design.ab"	"design.alpha"	"design.bib"	"design.crd"
[5] "design.cyclic"	"design.dau"	"design.graeco"	"design.lattice"
[9] "design.lsd"	"design.rcbd"	"design.split"	"design.strip"

For the use of symbols that do not appear in the keyboard in Spanish, such as: ~, [, ], &, ^, |, <, >, {, }, % or others, use the table 6.10.

## 2 DESCRIPTIVE STATISTICS

The package 'agricolae' provides some complementary functions to the R program, specifically for the management of the histogram.

### 2.1 HISTOGRAM

The histogram is constructed with the function `graph.freq()` and is associated to other functions: `polygon.freq`, `table.freq`, `stat.freq`, `intervals.freq`, `sturges.freq`, `join.freq`, `ojiva.freq`, and `normal.freq`.

Example 1.1 Data generated in R. (students' weight). Figure 2.1

```
c( 68, 53, 69.5, 55, 71, 63, 76.5, 65.5, 69, 75, 76, 57, 70.5, 71.5,
56, 81.5, 69, 59, 67.5, 61, 68, 59.5, 56.5, 73, 61, 72.5, 71.5,
59.5, 74.5, 63)-> weight
```

Load the package 'agricolae':

```
library(agricolae)
par(mfrow=c(2,2),cex=0.7)
h1<- graph.freq(weight, col="yellow", frequency =1, main="Absolute
frequency", axes=FALSE)
axis(1,h1$breaks)
axis(2,0:10)
h2<- graph.freq(weight, frequency =2, main=" polygon of frequency",
axes=FALSE)
axis(1,h2$breaks)
axis(2,seq(0,0.3,0.1))
polygon.freq(h2, col="blue", lwd=2, frequency =2)
h3<- graph.freq(weight, col="brown", frequency =3, main="density",
axes=FALSE)
axis(1,h3$breaks)
h4<- graph.freq(weight, col="blue", frequency =3, main=" normal
density", density=4, axes=FALSE)
axis(1,h4$breaks)
normal.freq(h4, col="red", lty=4,lwd=2, frequency=3)
```

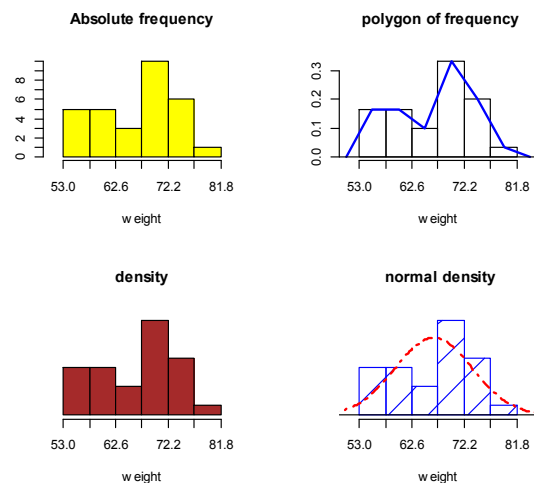
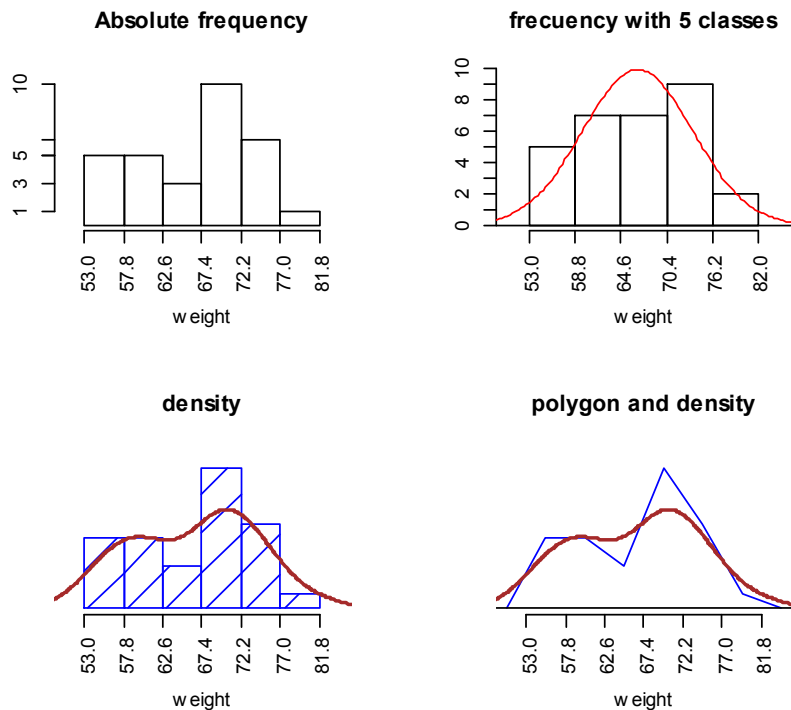


Figure 2.1 Histograms, polygon and density

## 2.2 HANDLING SCALES

It refers to the scale changes in the axes. Figure 2.2

```
par(mfrow=c(2,2),cex=0.7)
h5<- graph.freq(weight, axes=FALSE, frequency =1, main="Absolute
frequency")
axis(1,h5$breaks,las=2)
axis(2,h5$count)
h6<- graph.freq(weight, axes=FALSE, nclass=5, main="frequency with 5
classes")
axis(1,h6$breaks,las=2)
axis(2,seq(0,10))
normal.freq(h6,col="red")
h7<- graph.freq(weight, density=6, col="blue", frequency =3,
main="density", axes=FALSE)
lines(density(weight),col="brown",lwd=2)
axis(1,h7$breaks,las=2)
h8<- graph.freq(weight, border=0, frequency =3, main="polygon and
density", axes=FALSE)
polygon.freq(h8,col="blue", frequency =3)
lines(density(weight),col="brown",lwd=2)
axis(1,h8$breaks,las=2)
```



**Figure 2.2. Scale change of the axes of coordinates**

```
h9<-ojiva.freq(h5,axes=FALSE,type="b", main="ojiva of h5",
col="red")
axis(2,round(h9[,2],1),las=2)
axis(1,round(h9[,1],1),las=2)
```

## 2.3 FREQUENCY TABLES AND STATISTICS

Rounded off to two decimals:								<code>stat.freq(h6)</code>		
<code>round(table.freq(h6), 2)</code>								\$variance		
								[1] 50.42133		
								\$mean		
								[1] 66.72667		
								\$median		
								[1] 67.08571		
								\$mode		
								[ - - ] mode		
								70.4 76.2 71.68889		

## 2.4 REPRODUCING HISTOGRAMS AND USE OF hist()

The class of `graph.freq()` is `graph.freq`. Figure 2.3

Reproducing the histogram `h6` (5 classes)

```
h10<-plot(h6, axes=FALSE, main="frequency with 5 classes")
axis(1,h6$breaks,las=2)
axis(2,seq(0,10))
normal.freq(h6,col="red")
round(summary(h6),2)
```

Lower	Upper	Main	freq	relative	CF	RCF
53.0	58.8	55.9	5	0.17	5	0.17
58.8	64.6	61.7	7	0.23	12	0.40
64.6	70.4	67.5	7	0.23	19	0.63
70.4	76.2	73.3	9	0.30	28	0.93
76.2	82.0	79.1	2	0.07	30	1.00

The class types of the functions `hist()` and `graph.freq()` are 'histogram' and 'graph.freq', respectively. However, it is possible to establish compatibility between both functions.

```
hh <- hist(weight,nclass=5, plot=FALSE) # Reports 7 classes
# hist(weight,nclass=4) # Reports 4 classes
```

In order to show the relative frequencies, you can use `graph.freq()` with the object `hh` created by `hist()`, without modifying the classes.

```
h11<-graph.freq(hh, frequency=2,
col=colors()[367],main="relative",axes=F)
axis(1,h11$breaks,las=2)
axis(2,round(h11$relative,2),las=2)
```

See the summaries: `> summary(hh)`, `summary(h11)`

The functions of 'agricolae' for the management of histograms function correctly on the objects created by the function `hist()` of R.



## 2.5 HISTOGRAM BASED ON GROUPED DATA

If there are grouped data, you can graphic and obtain the histogram summaries with the function `graph.freq()`, as, for example, in the following table:

0-10	10-20	20-30	30-40	40-50
3	8	15	18	6

In R we have:

```
classes <- c(0, 10, 20, 30, 40, 50)
freq <- c(3, 8, 15, 18, 6)
h12 <- graph.freq(classes, counts=freq, xlab="Classes",
main="Classes")
summary(h12)
```

Lower	Upper	Main	freq	relative	CF	RCF
0	10	5	3	0.06	3	0.06
10	20	15	8	0.16	11	0.22
20	30	25	15	0.30	26	0.52
30	40	35	18	0.36	44	0.88
40	50	45	6	0.12	50	1.00

All the functions of 'agricolae' can be applied, including `plot()`.

```
plot(h11, frequency=2, col=colors()[367], main="relative", axes=F)
axis(1, h11$breaks, las=2)
axis(2, round(h11$relative, 2), las=2)
plot(h12, xlab="Classes", main="Classes")
```

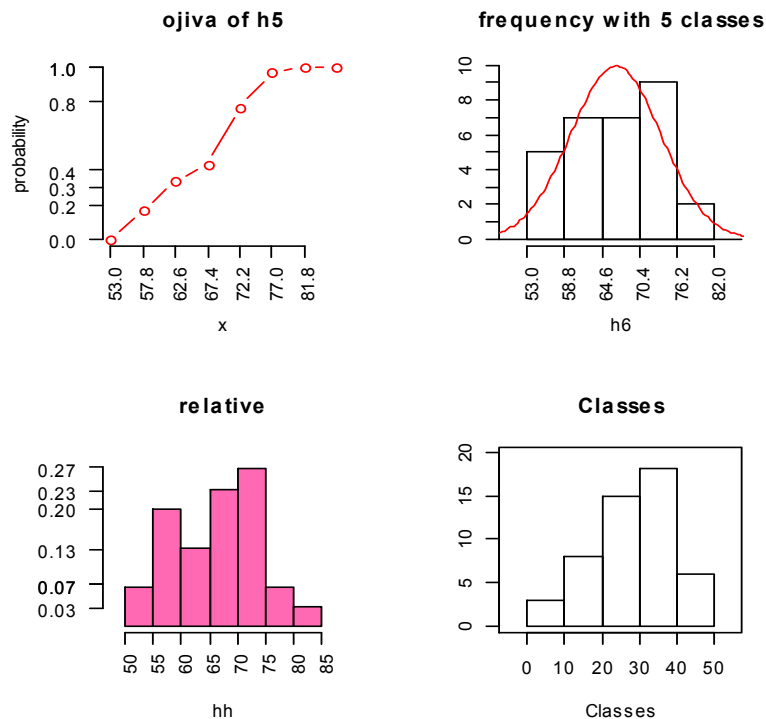


Figure 2.3 New scales for the histograms

## 2.6 JOINING CLASSES

Knowing the students' weight, the original intervals can be changed, joining, for example:

<pre>intervals.freq(h5\$breaks)</pre>	<pre>nuevas&lt;- join.freq(h5\$breaks,1:2) intervals.freq(nuevas)</pre>
<pre>      lower upper [1,]  53.2  58.0 [2,]  58.0  62.8 [3,]  62.8  67.6 [4,]  67.6  72.4 [5,]  72.4  77.2 [6,]  77.2  82.0</pre>	<pre>      lower upper [1,]  53.2  62.8 [2,]  62.8  67.6 [3,]  67.6  72.4 [4,]  72.4  77.2 [5,]  77.2  82.0</pre>
	<pre>h13 &lt;- graph.freq(peso, breaks=nuevas)</pre>

## 3 EXPERIMENT DESIGNS

The package 'agricolae' presents special functions for the creation of the field book for experimental designs. Due to the random generation, this package is quite used in agricultural research.

For this generation, certain parameters are required, as for example the name of each treatment, the number of repetitions, and others, according to the design (Cochran, 1992; Kuehl, 2000; Montgomery, 2002; LeClerg, 1962). There are other parameters of random generation, as the seed to reproduce the same random generation or the generation method (See the reference manual of agriculture <http://cran.at.r-project.org/web/packages/agricolae/agricolae.pdf>)

### 3.1 COMPLETELY RANDOMIZED DESIGNS

They only require the names of the treatments and the number of their repetitions.

```
trt <- c("A", "B", "C")
repetition <- c(4, 3, 4)
plan1 <- design.crd(trt,r=repetition)
```

```
      plots trt r
1         1   A 1
2         2   C 1
3         3   A 2
4         4   A 3
5         5   B 1
6         6   C 2
7         7   C 3
8         8   B 2
9         9   A 4
10        10   B 3
11        11   C 4
```

Excel:

```
write.csv(plan1,"plan1.csv",row.names=FALSE)
```

### 3.2 RANDOMIZED COMPLETE BLOCK DESIGN

They require the names of the treatments and the number of blocks.

```
trt <- c("A", "B", "C")
repetition <- 4
plan2 <- design.rcbd(trt,r=repetition, seed=5, number=101,
first=FALSE)
t(matrix(plan2[,3],c(3,4)))
      [,1] [,2] [,3]
[1,] "A"  "B"  "C"
[2,] "C"  "A"  "B"
[3,] "C"  "A"  "B"
[4,] "A"  "C"  "B"
```

The plan can be sent to excel as a field book.

### 3.3 LATIN SQUARE DESIGNS

They require the names of the treatments.

```
trt <- c("A", "B", "C", "D")
plan3 <- design.lsd(trt, seed=55, number=101, first=FALSE)
t(matrix(plan3[,4],c(4,4)))
      [,1] [,2] [,3] [,4]
[1,] "A"  "B"  "D"  "C"
[2,] "B"  "C"  "A"  "D"
[3,] "D"  "A"  "C"  "B"
[4,] "C"  "D"  "B"  "A"
```

### 3.4 GRAECO-LATIN DESIGNS

They require the names of the treatments of each factor of study.

```
T1 <- c("A", "B", "C", "D")
T2 <- 1:4
plan4 <- design.graeco(T1,T2, seed=55, number=101)
t(matrix(paste(plan4[,4],plan4[,5] ),c(4,4)))
      [,1] [,2] [,3] [,4]
[1,] "A 3" "D 4" "C 1" "B 2"
[2,] "D 1" "A 2" "B 3" "C 4"
[3,] "C 2" "B 1" "A 4" "D 3"
[4,] "B 4" "C 3" "D 2" "A 1"
```

### 3.5 BALANCED INCOMPLETE BLOCK DESIGNS

They require the names of the treatments and the size of the block.

```
trt <- c("A", "B", "C", "D", "Control")
k <- 4
plan5 <- design.bib(trt,k, seed=55, number=101)
```

```

Parameters BIB
=====
Lambda      : 3
treatments  : 5
Block size  : 4
Blocks      : 5
Replication : 4

Efficiency factor 0.9375

<<< Book >>>

```

According to the produced information, they are five blocks of size 4, being the matrix:

```

t(matrix(plan5[,3],c(4,5)))
      [,1]      [,2]      [,3]      [,4]
[1,] "B"      "Control" "C"      "A"
[2,] "D"      "A"      "C"      "B"
[3,] "B"      "C"      "Control" "D"
[4,] "C"      "D"      "A"      "Control"
[5,] "Control" "B"      "D"      "A"

```

It can be observed that the treatments have four repetitions. The parameter lambda has three repetitions, which means that a couple of treatments are together on three occasions. For example, B and E are found in the blocks I, III and V.

### 3.6 CYCLIC DESIGNS

They require the names of the treatments, the size of the block and the number of repetitions. This design is used for 6 to 30 treatments. The repetitions are a multiple of the size of the block; if they are six treatments and the size is 3, then the repetitions can be 6, 9, 12, etc.

```

trt <- c("A", "B", "C", "D", "E", "F")
plan5 <- design.cyclic(trt,k=3, r=6, seed=55, number=101)

```

```

cyclic design
Generator block basic:
1 2 4
1 3 2

```

```

Parameters
=====
treatments: 6
Block size: 3
Replication: 6

```

```

> plan5$design[[1]]
      [,1] [,2] [,3]
[1,] "F"  "A"  "C"
[2,] "A"  "D"  "B"
[3,] "B"  "C"  "E"
[4,] "D"  "F"  "C"
[5,] "A"  "D"  "E"
[6,] "B"  "E"  "F"

```

```
> plan5$design[[2]]
      [,1] [,2] [,3]
[1,] "D"  "E"  "C"
[2,] "E"  "F"  "D"
[3,] "B"  "C"  "D"
[4,] "A"  "F"  "E"
[5,] "C"  "B"  "A"
[6,] "B"  "F"  "A"
```

12 blocks of 4 treatments each have been generated.

### 3.7 LATTICE DESIGNS

They require a number of treatments of a perfect square; for example 9, 16, 25, 36, 49, etc.

They can generate a simple lattice (2 rep.) or a triple lattice (3 rep.)

generating a triple lattice design for 9 treatments 3x3

```
plan6 <- design.lattice(k=3, seed=55, number=101)
```

```
print(plan6)
```

```
$square1
      [,1] [,2] [,3]
[1,]     1     4     8
[2,]     2     9     3
[3,]     5     7     6
$square2
      [,1] [,2] [,3]
[1,]     2     1     5
[2,]     9     4     7
[3,]     3     8     6
$square3
      [,1] [,2] [,3]
[1,]     2     4     6
[2,]     3     1     7
[3,]     9     8     5

$plan
      plots sqr block trt
1       101     1     1   1
2       102     1     1   4
...
27      127     3     9   5
```

### 3.8 ALPHA DESIGNS

These designs are generated by the alpha arrangements (Patterson & Williams, 1976). They are similar to the lattice designs, but the tables are rectangular, with  $s$  blocks  $\times$   $k$  treatments. The number of treatments should be equal to  $s \times k$  and all the experimental units,  $r \times s \times k$ .

```
Genotype<-paste("geno", 1:15, sep = "")
plan7 <- design.alpha(Genotype,k=3,r=2,seed=55)
```

```
alpha design (0,1) - Serie I
```

```
Parameters Alpha design
```

```
=====
```

```
treatmeans : 15
```

```
Block size : 3
```

```
Blocks      : 5
```

```
Replication: 2
```

```
Efficiency factor
```

```
(E ) 0.6363636
```

```
<<< Book >>>
```

```
plan7$design$rep1
```

```
      [,1]      [,2]      [,3]  
[1,] "geno8"  "geno4"  "geno10"  
[2,] "geno1"  "geno12" "geno14"  
[3,] "geno6"  "geno2"  "geno15"  
[4,] "geno7"  "geno3"  "geno11"  
[5,] "geno13" "geno9"  "geno5"
```

```
plan7$design$rep2
```

```
      [,1]      [,2]      [,3]  
[1,] "geno13" "geno7"  "geno1"  
[2,] "geno8"  "geno5"  "geno14"  
[3,] "geno4"  "geno11" "geno15"  
[4,] "geno6"  "geno3"  "geno12"  
[5,] "geno10" "geno2"  "geno9"
```

### 3.9 AUGMENTED BLOCK DESIGNS

These are designs for two types of treatments: the control treatments (common) and the increased treatments. The common treatments are applied in complete randomized blocks, and the increased treatments, at random. Each treatment should be applied in any block once only. It is understood that the common treatments are of a greater interest; the standard error of the difference is much smaller than when between two increased ones in different blocks. The function `design.dau()` achieves this purpose.

```
common <- c("A", "B", "C", "D")  
others <- c("t", "u", "v", "w", "x", "y", "z")  
plan8 <- design.dau(common,others, r=5, seed=55, number=101)  
by(plan8$trt, plan8$block,function(x) as.character(x))  
block: 1  
[1] "D" "A" "v" "C" "B" "u"  
-----  
block: 2  
[1] "t" "D" "A" "x" "B" "C"  
-----  
block: 3  
[1] "D" "C" "B" "A" "w"  
-----  
block: 4  
[1] "A" "C" "D" "B" "y"  
-----
```

```
block: 5
[1] "z" "A" "B" "D" "C"
```

```
print(plan8)
```

```
      plots block trt
1      101      1   A
2      102      1   t
3      103      1   B
4      104      1   D
...
32     132      5   D
```

For augmented randomized complete block designs, use the function `design.crd()`.

### 3.10 SPLIT-PLOT DESIGNS

These designs have two factors, one is applied in plots and is defined as A in a randomized complete block design; and a second factor, which is applied in the subplots of each plot applied at random. The function `design.split()` permits to find the experimental plan for this design.

```
t1<-c("A", "B", "C", "D")
t2<-c("a", "b", "c")
plan9 <-design.split(t1,t2,r=3,number=101,seed=45, first=FALSE)
print(plan9)
      plots block t1 t2
1      101      1  A  b
2      101      1  A  a
3      101      1  A  c
4      102      1  B  c
. . .
36     112      3  D  c
p<-plan9$t1[seq(1,36,3)]
q<-NULL
for(i in 1:12) q<-c(q,paste(plan9$t2[3*(i-1)+1],plan9$t2[3*(i-1)+2],plan9$t2[3*(i-1)+3]))
```

In the plots

```
> print(t(matrix(p,c(4,3)) ))
      [,1] [,2] [,3] [,4]
[1,] "A"  "B"  "C"  "D"
[2,] "B"  "D"  "C"  "A"
[3,] "A"  "B"  "C"  "D"
> print(t(matrix(q,c(4,3)) ))
      [,1] [,2] [,3] [,4]
[1,] "b a c" "c b a" "a b c" "b a c"
[2,] "a c b" "a c b" "b a c" "b a c"
[3,] "c b a" "c a b" "a c b" "a b c"
```

### 3.11 STRIP-PLOT DESIGNS

These designs are used when there are two types of treatments (factors) and are applied separately in large plots, called bands, in a vertical and horizontal direction of the block, obtaining the divided blocks. Each block constitutes a repetition.

```
t1<-c("A", "B", "C")
t2<-c("a", "b", "c", "d")
```

```
plan10 <-design.strip(t1,t2,r=3,number=101,seed=45)
print(plan10)
```

```
      plots block t1 t2
1      101      1  B  b
2      102      1  B  a
3      103      1  B  d
4      104      1  B  c
...
36     136      3  A  c
```

```
t3<-paste(plan10$t1,plan10$t2)
B1<-t(matrix(t3[1:12],c(4,3)))
B2<-t(matrix(t3[13:24],c(4,3)))
B3<-t(matrix(t3[25:36],c(4,3)))
```

```
> print(B1)
      [,1] [,2] [,3] [,4]
[1,] "B b" "B a" "B d" "B c"
[2,] "C b" "C a" "C d" "C c"
[3,] "A b" "A a" "A d" "A c"
> print(B2)
      [,1] [,2] [,3] [,4]
[1,] "A c" "A a" "A d" "A b"
[2,] "C c" "C a" "C d" "C b"
[3,] "B c" "B a" "B d" "B b"
> print(B3)
      [,1] [,2] [,3] [,4]
[1,] "B d" "B a" "B b" "B c"
[2,] "C d" "C a" "C b" "C c"
[3,] "A d" "A a" "A b" "A c"
```

## 4 MULTIPLE COMPARISONS

For the analyses, the following functions of 'agricolae' are used: `LSD.test()`, `HSD.test()`, `duncan.test()`, `scheffe.test`, `waller.test`, `SNK.test()` (Steel, 1996) and `durbin.test()`, `kruskal()`, `friedman()` and `waerden.test` (Conover, 1999).

For every statistical analysis, the data should be organized in columns. For the demonstration, the 'agricolae' database will be used.

The 'sweetpotato' data correspond to a completely random experiment in field with plots of 50 sweet potato plants, subjected to the virus effect and to a control without virus (See the reference manual of the package).

```
data(sweetpotato)
model<-aov(yield~virus, data=sweetpotato)

cv.model(model)
[1] 17.16660
attach(sweetpotato)
mean(yield)
[1] 27,625
```

Model parameters: Degrees of freedom and variance of the error:



```
df<-df.residual(model)
MSerror<-deviance(model)/df
```

#### 4.1 THE LEAST SIGNIFICANT DIFFERENCE (LSD)

It includes the multiple comparison through the method of the minimum significant difference (Least Significant Difference), (Steel, 1997).

```
# comparison <- LSD.test(yield,virus,df,MSerror)
LSD.test(model, "virus")
Study:
```

LSD t Test for yield

Mean Square Error: 22.48917

virus, means and individual ( 95 %) CI

	yield	std.err	replication		LCL	UCL
cc	24.40000	2.084067	3	19.594134	29.20587	
fc	12.86667	1.246774	3	9.991602	15.74173	
ff	36.33333	4.233727	3	26.570341	46.09633	
oo	36.90000	2.482606	3	31.175100	42.62490	

alpha: 0.05 ; Df Error: 8  
Critical Value of t: 2.306004

Least Significant Difference 8.928965  
Means with the same letter are not significantly different.

Groups, Treatments and means

a	oo	36.9
a	ff	36.33
b	cc	24.4
c	fc	12.87

In the function LSD.test(), the multiple comparison was carried out. In order to obtain the probabilities of the comparisons, it should be indicated that groups are not required; thus:

```
# compara <- LSD.test(yield, virus,df, MSerror, group=F)
LSD.test(model, "virus", group=F)
```

LSD t Test for yield

Mean Square Error: 22.48917

virus, means and individual ( 95 %) CI

	yield	std.err	replication		LCL	UCL
cc	24.40000	2.084067	3	19.594134	29.20587	
fc	12.86667	1.246774	3	9.991602	15.74173	
ff	36.33333	4.233727	3	26.570341	46.09633	
oo	36.90000	2.482606	3	31.175100	42.62490	

alpha: 0.05 ; Df Error: 8  
Critical Value of t: 2.306004

Comparison between treatments means

	Difference	pvalue	sig	LCL	UCL
cc - fc	11.5333333	0.0176377595	*	2.604368	20.462299
cc - ff	-11.9333333	0.0150730851	*	-20.862299	-3.004368
cc - oo	-12.5000000	0.0120884239	*	-21.428965	-3.571035
fc - ff	-23.4666667	0.0003023690	***	-32.395632	-14.537701
fc - oo	-24.0333333	0.0002574929	***	-32.962299	-15.104368
ff - oo	-0.5666667	0.8872673216		-9.495632	8.362299

The significance code “sig” is interpreted as:

```

"***": p.valor < 0.001
"*** ": 0.001 < p.valor < 0.01
"*  ": 0.01 < p.valor < 0.05
".  ": 0.05 < p.valor < 0.10

```

## 4.2 BONFERRONI

With the function `LSD.test()` we can make adjustments to the probabilities found, as for example the adjustment by Bonferroni.

```
LSD.test(model, "virus", group=F, p.adj= "bon")
```

LSD t Test for yield  
P value adjustment method: bonferroni

alpha: 0.05 ; Df Error: 8  
Critical Value of t: 3.478879

Comparison between treatments means

	Difference	pvalue	sig	LCL	UCL
cc - fc	11.5333333	0.105827		-1.937064	25.0037305
cc - ff	-11.9333333	0.090439	.	-25.403730	1.5370638
cc - oo	-12.5000000	0.072531	.	-25.970397	0.9703971
fc - ff	-23.4666667	0.001814	**	-36.937064	-9.9962695
fc - oo	-24.0333333	0.001545	**	-37.503730	-10.5629362
ff - oo	-0.5666667	1.000000		-14.037064	12.9037305

Other comparison tests can be applied, such as “duncan”, “Student-Newman-Keuls”, “tukey”, and “waller-duncan.”

For “duncan”, use the function `duncan.test()`; for “Student-Newman-Keuls”, the function `SNK.test()`; for “tukey”, the function `HSD.test()`; for “scheffe”, the function `scheffe.test()`; and for “waller-duncan”, the function `waller.test()`. The parameters are the same. “Waller” also requires the value of F-calculated of the ANOVA treatments. If the model is used as a parameter, this is no longer necessary.

### 4.3 DUNCAN'S NEW MULTIPLE-RANGE TEST

It corresponds to the Duncan's Test (Steel, 1997).

```
duncan.test(model, "virus")
```

Duncan's new multiple range test  
for yield

Mean Square Error: 22.48917

virus, means

	yield	std.err	replication
cc	24.40000	2.084067	3
fc	12.86667	1.246774	3
ff	36.33333	4.233727	3
oo	36.90000	2.482606	3

alpha: 0.05 ; Df Error: 8

Critical Range

	2	3	4
	8.928965	9.304825	9.514910

Means with the same letter are not significantly different.

Groups, Treatments and means

a	oo	36.9
a	ff	36.33
b	cc	24.4
c	fc	12.87

```
duncan.test(model, "virus", group=FALSE)
```

Duncan's new multiple range test  
for yield

Mean Square Error: 22.48917

alpha: 0.05 ; Df Error: 8

Critical Range

	2	3	4
	8.928965	9.304825	9.514910

Comparison between treatments means

	Difference	pvalue	sig	LCL	UCL
cc - fc	11.5333333	0.017638	*	2.604368	20.462299
cc - ff	-11.9333333	0.015073	*	-20.862299	-3.004368
cc - oo	-12.5000000	0.014544	*	-21.804825	-3.195175
fc - ff	-23.4666667	0.000388	***	-32.771492	-14.161842
fc - oo	-24.0333333	0.000387	***	-33.548244	-14.518423
ff - oo	-0.5666667	0.887267		-9.495632	8.362299

#### 4.4 STUDENT-NEWMAN-KEULS

Student, Newman and Keuls helped to improve the Newman-Keuls test of 1939, which was known as the Keuls method (Steel, 1997).

```
SNK.test(model, "virus", alpha=0.05)
```

```
Student Newman Keuls Test  
for yield
```

```
Mean Square Error: 22.48917
```

```
virus, means
```

	yield	std.err	replication
cc	24.40000	2.084067	3
fc	12.86667	1.246774	3
ff	36.33333	4.233727	3
oo	36.90000	2.482606	3

```
alpha: 0.05 ; Df Error: 8
```

```
Critical Range  
      2      3      4  
8.928965 11.064170 12.399670
```

Means with the same letter are not significantly different.

```
Groups, Treatments and means  
a      oo      36.9  
a      ff      36.33  
b      cc      24.4  
c      fc      12.87
```

```
SNK.test(model, "virus", group=FALSE)
```

```
Student Newman Keuls Test  
for yield
```

```
Mean Square Error: 22.48917
```

```
alpha: 0.05 ; Df Error: 8
```

```
Critical Range  
      2      3      4  
8.928965 11.064170 12.399670
```

```
Comparison between treatments means
```

	Difference	pvalue	sig	LCL	UCL
cc-fc	11.5333333	0.017638	*	2.604368	20.462299
cc-ff	-11.9333333	0.015073	*	-20.862299	-3.004368
cc-oo	-12.5000000	0.029089	*	-23.564170	-1.435830
fc-ff	-23.4666667	0.000777	***	-34.530836	-12.402497
fc-oo	-24.0333333	0.001162	**	-36.433003	-11.633664
ff-oo	-0.5666667	0.887267		-9.495632	8.362299

#### 4.5 TUKEY'S W PROCEDURE (HSD)

This studentized range test, created by Tukey in 1953, is known as the Tukey's HSD (Honestly Significant Differences) Test (Steel, 1997).

```
comparison1 <- HSD.test(model, "virus")
```

HSD Test for yield

Mean Square Error: 22.48917

virus, means

	yield	std.err	replication
cc	24.40000	2.084067	3
fc	12.86667	1.246774	3
ff	36.33333	4.233727	3
oo	36.90000	2.482606	3

alpha: 0.05 ; Df Error: 8

Critical Value of Studentized Range: 4.52881

Honestly Significant Difference: 12.39967

Means with the same letter are not significantly different.

Groups, Treatments and means

a	oo	36.9
ab	ff	36.33
bc	cc	24.4
c	fc	12.87

```
comparison1
```

	trt	means	M	N	std.err
1	oo	36.90000	a	3	2.482606
2	ff	36.33333	ab	3	4.233727
3	cc	24.40000	bc	3	2.084067
4	fc	12.86667	c	3	1.246774

#### 4.6 WALLER-DUNCAN'S BAYESIAN K-RATIO t-TEST

In 1975, Duncan continued the multiple comparison procedures, introducing the criterion of minimizing both experimental errors; for this, he used the Bayes' theorem, obtaining one new test called Waller-Duncan (Steel, 1997).

```
# variance analysis:
```

```
anova(model)
```

Analysis of Variance Table

Response: yield

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
virus	3	1170.21	390.07	17.345	0.0007334 ***
Residuals	8	179.91	22.49		

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

The value of calculated F is 17,345. For the comparative treatment analysis, it is required that 'sweetpotato' be active, thus:

```
attach(sweetpotato)
```

then:

```
waller.test(yield,virus,df,MSError,Fc= 17.345, group=F)
```

In another case with only invoking the `model` object:

```
comparison2 <- waller.test(model, "virus", group=F)
```

Waller-Duncan K-ratio t Test for yield

This test minimizes the Bayes risk under additive loss and certain other assumptions.

```

      . . . . .
K ratio          100.00000
Error Degrees of Freedom    8.00000
Error Mean Square          22.48917
F value                17.34478
Critical Value of Waller    2.23600

```

virus, means

	yield	std.err	replication
cc	24.40000	2.084067	3
fc	12.86667	1.246774	3
ff	36.33333	4.233727	3
oo	36.90000	2.482606	3

Minimum Significant Difference 8.657906  
Comparison between treatments means

	Difference	significant
cc - fc	11.5333333	TRUE
ff - cc	11.9333333	TRUE
oo - cc	12.5000000	TRUE
ff - fc	23.4666667	TRUE
oo - fc	24.0333333	TRUE
oo - ff	0.5666667	FALSE

It is indicated that the virus effect "ff" is not significant to the control "oo."

The found object "compara" has information to make other procedures.

```
comparison2
```

	trt	means	M	N	std.err
1	cc	24.40000	3	2.084067	
2	fc	12.86667	3	1.246774	
3	ff	36.33333	3	4.233727	
4	oo	36.90000	3	2.482606	

## 4.7 SCHEFFE'S TEST

This method, created by Scheffe in 1959, is very general for all the possible contrasts and their confidence intervals. The confidence intervals for the averages are very broad, resulting in a very conservative test for the comparison between treatment averages (Steel, 1997).

```
# analysis of variance:
model<-aov(yield~virus, data=sweetpotato)
scheffe.test(model,"virus", group=TRUE,
main="Yield of sweetpotato\nDealt with different virus")
```

```
Study: Yield of sweetpotato
Dealt with different virus
```

```
Scheffe Test for yield
```

```
Mean Square Error   : 22.48917
```

```
virus, means
```

	yield	std.err	replication
cc	24.40000	2.084067	3
fc	12.86667	1.246774	3
ff	36.33333	4.233727	3
oo	36.90000	2.482606	3

```
alpha: 0.05 ; Df Error: 8
Critical Value of F: 4.066181
```

```
Minimum Significant Difference: 13.52368
```

```
Means with the same letter are not significantly different.
```

```
Groups, Treatments and means
```

a	oo	36.9
a	ff	36.33
ab	cc	24.4
b	fc	12.87

The minimum significant value is very high.

If you require the approximate probabilities of comparison, you can use the option Group=FALSE.

```
comparison3 <- scheffe.test(model,"virus", group=FALSE)
```

```
Study:
```

```
Scheffe Test for yield
```

```
Mean Square Error   : 22.48917
```

```
virus, means
```

	yield	std.err	replication
cc	24.40000	2.084067	3
fc	12.86667	1.246774	3

```
ff 36.33333 4.233727      3
oo 36.90000 2.482606      3
```

alpha: 0.05 ; Df Error: 8  
Critical Value of F: 4.066181

Comparison between treatments means

	Difference	pvalue	sig	LCI	UCL
cc - fc	11.5333333	0.097816	.	-1.000348	24.0670149
cc - ff	-11.9333333	0.085487	.	-24.467015	0.6003483
cc - oo	-12.5000000	0.070607	.	-25.033682	0.0336816
fc - ff	-23.4666667	0.002331	**	-36.000348	-10.9329851
fc - oo	-24.0333333	0.001998	**	-36.567015	-11.4996517
ff - oo	-0.5666667	0.999099		-13.100348	11.9670149

## 4.8 GRAPHICS OF THE MULTIPLE COMPARISON

The results of a comparison can be graphically seen with the functions `bar.group()` and `bar.err()`.

The found object of one comparison is the entry for these functions, Figure 4.1.

The objects `compara1` and `compara2` are used in the following exercise:

`compara1`, for the functions `bar.group()` and `bar.err()`  
`compara2`, for the function `bar.err()`

```
par(mfrow=c(2,2))
c1<-colors()[480]; c2=colors()[65]; c3=colors()[15];
c4=colors()[140]
G1<-bar.group(comparison1, ylim=c(0,45), main="Tukey\nG1",col=c1)
G2<-bar.group(comparison1, horiz=T, xlim=c(0,45),
main="Tukey\nG2",col=c2)
G3<-bar.err(comparison2, ylim=c(0,45), col=c3, main="Standard
deviation\nG3")
G4<-bar.err(comparison2, horiz=T, xlim=c(0,45), col=c4,
std=F,main="Standard error \nG4")
```

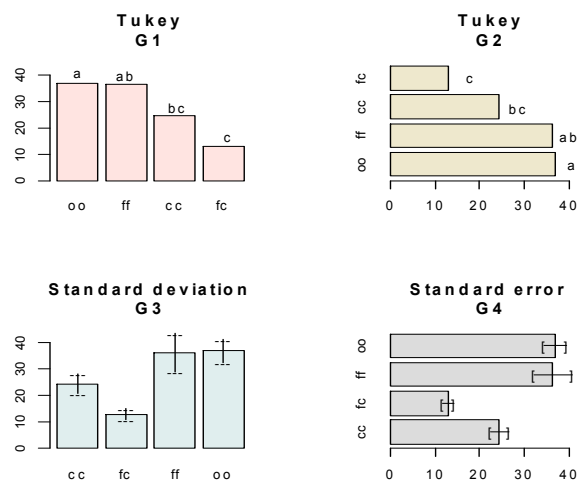


Figure 4.1 Comparison between treatments



## 4.9 ANALYSIS OF BALANCED INCOMPLETE BLOCKS

This analysis can come from balanced or partially balanced designs. The function `BIB.test()` is for balanced designs, and `PBIB.test()`, for partially balanced designs. In the following example, the 'agricolae' data will be used.

```
#Example linear estimation and design of experiments. (Joshi, 1987)
# Profesor de Estadística, Institute of Social Sciences Agra, India
# 6 variedades de trigo en 10 bloques de 3 parcelas cada una.
block<-gl(10,3)
variety<-c(1,2,3,1,2,4,1,3,5,1,4,6,1,5,6,2,3,6,2,4,5,2,5,6,3,4,5,3,
4,6)
y<-c(69,54,50,77,65,38,72,45,54,63,60,39,70,65,54,65,68,67,57,60,62,
59,65,63,75,62,61,59,55,56)
```

```
BIB.test(block, variety, y)
```

```
ANALYSIS BIB: y
Class level information
```

```
Block:  1 2 3 4 5 6 7 8 9 10
Trt  :  1 2 3 4 5 6
```

```
Number of observations:  30
```

```
Analysis of Variance Table
```

```
Response: y
```

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
block.unadj	9	466.97	51.885	0.9019	0.54712
trt.adj	5	1156.44	231.289	4.0206	0.01629 *
Residuals	15	862.89	57.526		

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
coefficient of variation: 12.6 %
y Means: 60.3
```

```
variety,  statistics
```

	means	mean.adj	StdError.adj
1	70.2	75.13333	3.728552
2	60.0	58.71667	3.728552
3	59.4	58.55000	3.728552
4	55.0	54.96667	3.728552
5	61.4	60.05000	3.728552
6	55.8	54.38333	3.728552

```
LSD test
```

```
Std.diff : 5.363111
Alpha    : 0.05
LSD      : 11.4312
```

```
Parameters BIB
```

```
Lambda    : 2
treatmeans : 6
Block size : 3
Blocks    : 10
```

Replication: 5

Efficiency factor 0.8

<<< Book >>>

Means with the same letter are not significantly different.

Comparison of treatments

Groups, Treatments and means

a	1	75.13
b	5	60.05
b	2	58.72
b	3	58.55
b	4	54.97
b	6	54.38

function (block, trt, y, method = c("lsd", "tukey", "duncan", "waller", "snk"), alpha = 0.05, group = TRUE). LSD, Tukey Duncan, Waller-Duncan and SNK, can be used. The probabilities of the comparison can also be obtained. It should only be indicated: group=FALSE, thus:

```
BIB.test(block=bloque, trt=variedad, y, group=F, method= "tukey")
```

```
Tukey
Alpha      : 0.05
Std.err    : 3.792292
HSD        : 17.42458
Parameters BIB
Lambda     : 2
treatmeans : 6
Block size : 3
Blocks     : 10
Replication: 5
```

Efficiency factor 0.8

<<< Book >>>

Comparison between treatments means

	Difference	pvalue	sig
1 - 2	16.4166667	0.070509	.
1 - 3	16.5833333	0.066649	.
1 - 4	20.1666667	0.019092	*
1 - 5	15.0833333	0.109602	
1 - 6	20.7500000	0.015510	*
2 - 3	0.1666667	1.000000	
2 - 4	3.7500000	0.979184	
2 - 5	-1.3333333	0.999840	
2 - 6	4.3333333	0.961588	
3 - 4	3.5833333	0.982927	
3 - 5	-1.5000000	0.999715	
3 - 6	4.1666667	0.967375	
4 - 5	-5.0833333	0.927273	
4 - 6	0.5833333	0.999997	
5 - 6	5.6666667	0.890815	

The found "model" object can be used for the functions `bar.group()` and `bar.err()` for the bar graphics, in the same way as previously.

#### 4.10 PARTIALLY BALANCED INCOMPLETE BLOCKS

The function `PBIB.test()` (Joshi, 1987) can be used for the lattice and alpha designs.

Consider the following case: Construct the alpha design with 30 treatments, 2 repetitions, and a block size equal to 3.

```
library(agricolae)
library(MASS)
library(lme4)
# alpha design
Genotype<-paste("geno",1:30,sep="")
r<-2
k<-3
plan<-design.alpha(Genotype,k,r,seed=5)
```

alpha design (0,1) - Serie I

Parameters Alpha design

```
=====
treatmeans : 30
Block size : 3
Blocks      : 10
Replication: 2
```

Efficiency factor  
(E ) 0.6170213

<<< Book >>>

The generated plan is `plan$book`.

Suppose that the corresponding observation to each experimental unit is:

```
yield <-c(5,2,7,6,4,9,7,6,7,9,6,2,1,1,3,2,4,6,7,9,8,7,6,4,3,2,2,1,1,
2,1,1,2,4,5,6,7,8,6,5,4,3,1,1,2,5,4,2,7,6,6,5,6,4,5,7,6,5,5,4)
```

The data table is constructed for the analysis. In theory, it is presumed that a design is applied and the experiment is carried out; subsequently, the study variables are observed from each experimental unit.

```
table<-data.frame(plan$book,yield)
rm(yield,Genotype)
```

The analysis:

```
attach(table)
model <- PBIB.test(block, Genotype, replication, yield, k=3,
group=TRUE)
detach(table)
```

ANALYSIS PBIB: yield

Class level information

block : 20

Genotype : 30

Number of observations: 60

Estimation Method: REML

Parameter Estimates

	Variance
block:replication	2.834033
replication	0.000000
Residual	2.003098

Fit Statistics

-2 Res Log Likelihood	147.6594
AIC	215.6594
BIC	286.8671

Analysis of Variance Table

Response: yield

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Genotype	29	72.006	2.4830	1.2396	0.3668
Residuals	11	22.034	2.0031		

coefficient of variation: 31.2 %

yield Means: 4.533333

Parameters PBIB

Genotype	30
block size	3
block/replication	10
replication	2

Efficiency factor 0.6170213

Means with the same letter are not significantly different.

Groups, Treatments and means

a	20	7.729
ab	13	6.715
ab	1	6.505
abc	8	6.192
abcd	24	6.032
abcd	23	5.735
abcd	10	5.473
abcd	16	5.455
abcd	21	5.14
abcd	22	5.069
abcd	4	4.874
abcd	3	4.794
abcd	14	4.742
abcd	15	4.587
abcd	27	4.563
abcd	7	4.424
abcd	5	4.286

abcd	19	4.198
abcd	6	4.165
abcd	25	3.978
abcd	17	3.943
bcd	2	3.628
bcd	28	3.495
bcd	11	3.379
bcd	26	3.341
bcd	9	3.052
bcd	30	3
bcd	12	2.879
cd	29	2.44
d	18	2.186

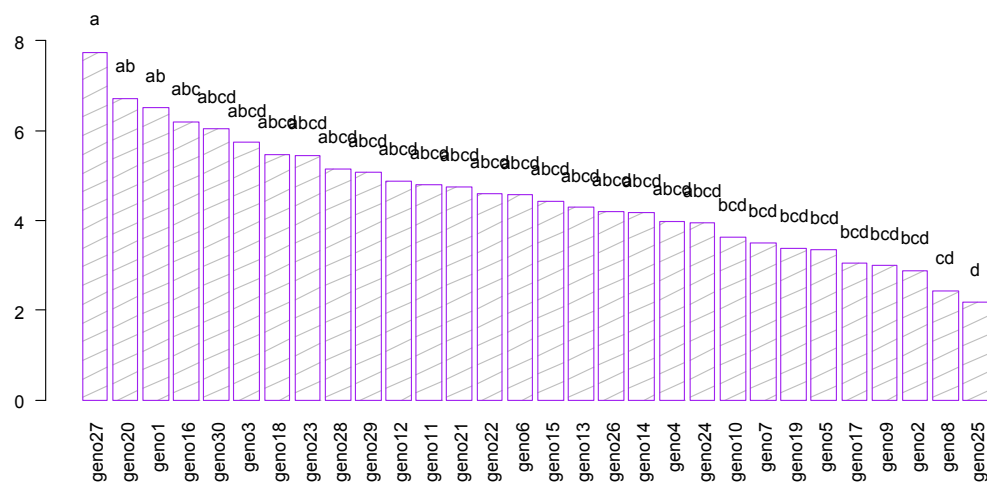
Comparison between treatments means and its name

<<< to see the objects: means, comparison and groups. >>>

The adjusted averages can be extracted from the model.

`model$means`

	trt	means	mean.adj	N	std.err
geno1	1	7.5	6.504752	2	1.313644
geno10	2	4.5	3.628197	2	1.313644
geno11	3	5.5	4.793619	2	1.310726
...					
geno7	28	2.0	3.495104	2	1.310726
geno8	29	3.0	2.439878	2	1.310726
geno9	30	3.5	2.999638	2	1.310726



**Figure 4.2. Treatment Groups.**

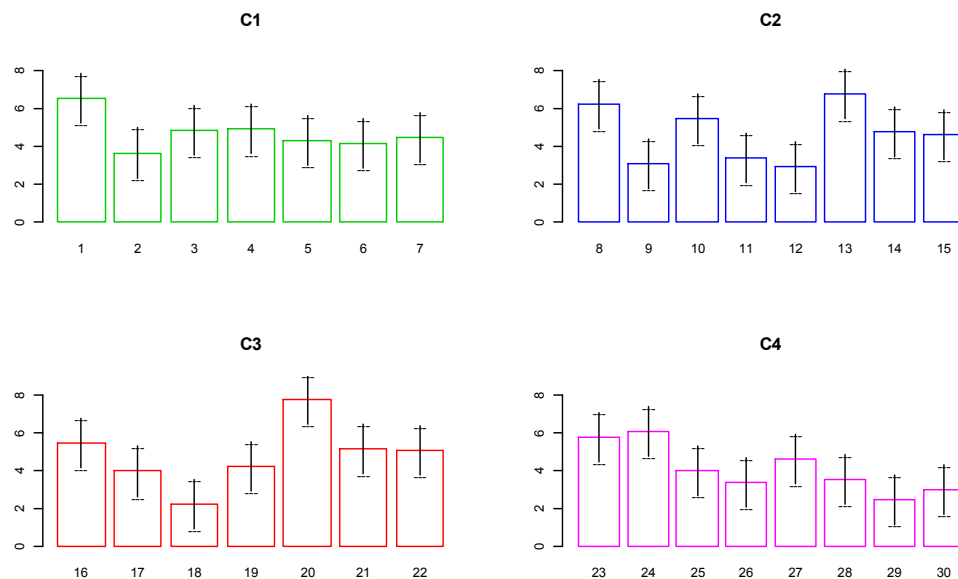
The comparisons:

```
model$comparison
```

	Difference	stderr	pvalue
1 - 2	2.87655507	1.844369	0.147134
1 - 3	1.71113250	1.576446	0.300944
1 - 4	1.63087260	1.727016	0.365282
1 - 5	2.21879565	1.853044	0.256324
....			
27 - 30	1.56381175	1.812351	0.406632
28 - 29	1.05522604	1.850095	0.579894
28 - 30	0.49546622	1.847786	0.793552
29 - 30	-0.55975982	1.587129	0.730988

The data on the adjusted averages and their standard error can be illustrated (figure 4.2), since the created object is very similar to the objects generated by the multiple comparisons.

```
par(mfrow=c(2,2),cex=0.6)
C1<-bar.err(model$means[1:7, c(1,3,2,4,5)], ylim=c(0,9), col=0,
main="C1", std=F,border=3)
C2<-bar.err(model$means[8:15, c(1,3,2,4,5)], ylim=c(0,9), col=0,
main="C2", std=F, border =4)
C3<-bar.err(model$means[16:22, c(1,3,2,4,5)], ylim=c(0,9), col=0,
main="C3", std=F, border =2)
C4<-bar.err(model$means[23:30, c(1,3,2,4,5)], ylim=c(0,9), col=0,
main="C4", std=F, border =6)
```



**Figure 4.3. Standard deviation in each treatment.**

Analysis of balanced lattice 3x3, 9 treatments, 4 repetitions.

Create the data in a text file: lattice3x3.txt and read with R:



Parameters PBIB

trt .  
block size 9  
block/sqr 3  
sqr 4

Efficiency factor 0.75

Means with the same letter are not significantly different.

Groups, Treatments and means

a	1	45.89
ab	9	39.61
ab	4	38.09
bc	7	31.9
bc	6	30.24
cd	2	25.67
d	8	18.71
d	5	16.9
d	3	15.44

Comparison between treatments means and its name

<<< to see the objects: means, comparison and groups. >>>

```
par(mar=c(3,3,0,0))  
bar.group(model2$group,ylim=c(0,52),density=10)
```

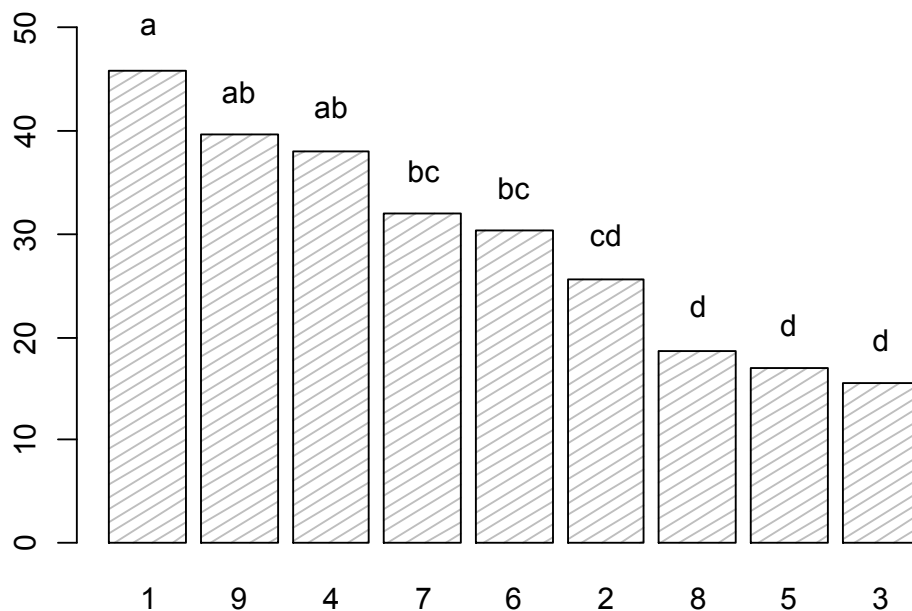


Figure 4.4. Treatment Groups.

model2\$means

	trt	means	mean.adj	N	std.err
1	1	45.8925	45.8925	4	3.772839
2	2	25.6675	25.6675	4	3.772839



```

3   3 15.4450  15.4450 4 3.772839
4   4 38.0875  38.0875 4 3.772839
5   5 16.9025  16.9025 4 3.772839
6   6 30.2425  30.2425 4 3.772839
7   7 31.9000  31.9000 4 3.772839
8   8 18.7075  18.7075 4 3.772839
9   9 39.6100  39.6100 4 3.772839

```

```
model2$comparison
```

```

      Difference   stderr   pvalue
1 - 2      20.2250 5.335599 0.001604
1 - 3      30.4475 5.335599 0.000032
1 - 4       7.8050 5.335599 0.162884
1 - 5      28.9900 5.335599 0.000056
.....
8 - 9     -20.9025 5.335599 0.001228

```

## 4.11 AUGMENTED BLOCKS

The function `DAU.test()` can be used for the analysis of the augmented block design.

The data should be organized in a table, containing the blocks, treatments, and the response.

```

block<-c(rep("I",7),rep("II",6),rep("III",7))
trt<-c("A","B","C","D","g","k","l","A","B","C","D","e","i","A","B",
"C","D","f","h","j")
yield<-c(83,77,78,78,70,75,74,79,81,81,91,79,78,92,79,87,81,89,96,
82)
data.frame(block, trt, yield)

```

	block	trt	yield
1	I	A	83
2	I	B	77
3	I	C	78
4	I	D	78
5	I	g	70
6	I	k	75
7	I	l	74
8	II	A	79
9	II	B	81
10	II	C	81
11	II	D	91
12	II	e	79
13	II	i	78
14	III	A	92
15	III	B	79
16	III	C	87
17	III	D	81
18	III	f	89
19	III	h	96
20	III	j	82

The treatments are in each block:

```

by(trt,block,as.character)
block: I
[1] "A" "B" "C" "D" "g" "k" "l"
-----
block: II
[1] "A" "B" "C" "D" "e" "i"
-----
block: III
[1] "A" "B" "C" "D" "f" "h" "j"

```

With their respective responses:

```

by(yield,block,as.character)
block: I
[1] 83 77 78 78 70 75 74
-----
block: II
[1] 79 81 81 91 79 78
-----
block: III
[1] 92 79 87 81 89 96 82

```

```
model<- DAU.test(block,trt,yield,method="lsd")
```

ANALYSIS DAU: yield  
Class level information

```

Block:  I II III
Trt   :  A B C D e f g h i j k l

```

Number of observations: 20

ANOVA, Treatment Adjusted  
Analysis of Variance Table

Response: yield

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
block.unadj	2	360.07	180.036		
trt.adj	11	285.10	25.918	0.9609	0.5499
Control	3	52.92	17.639	0.6540	0.6092
Control + control.VS.aug.	8	232.18	29.022	1.0760	0.4779
Residuals	6	161.83	26.972		

ANOVA, Block Adjusted  
Analysis of Variance Table

Response: yield

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
trt.unadj	11	575.67	52.333		
block.adj	2	69.50	34.750	1.2884	0.3424
Control	3	52.92	17.639	0.6540	0.6092
Augmented	7	505.88	72.268	2.6793	0.1253
Control vs augmented	1	16.88	16.875	0.6256	0.4591
Residuals	6	161.83	26.972		

coefficient of variation: 6.4 %  
yield Means: 81.5

Critical Differences (Between)	Std Error Diff.
Two Control Treatments	4.240458
Two Augmented Treatments (Same Block)	7.344688
Two Augmented Treatments(Different Blocks)	8.211611
A Augmented Treatment and A Control Treatment	6.360687

Means with the same letter are not significantly different.

Groups, Treatments and means

a	h	93.5
ab	f	86.5
ab	A	84.67
ab	D	83.33
ab	C	82
ab	j	79.5
ab	B	79
ab	e	78.25
ab	k	78.25
ab	i	77.25
ab	l	77.25
b	g	73.25

Comparison between treatments means

<<< to see the objects: pvalue and means >>>

`model$means`

	means	mean.adj	N	block	std.err
A	84.66667	84.66667	3		2.998456
B	79.00000	79.00000	3		2.998456
C	82.00000	82.00000	3		2.998456
D	83.33333	83.33333	3		2.998456
e	79.00000	78.25000	1	II	5.193479
f	89.00000	86.50000	1	III	5.193479
g	70.00000	73.25000	1	I	5.193479
h	96.00000	93.50000	1	III	5.193479
i	78.00000	77.25000	1	II	5.193479
j	82.00000	79.50000	1	III	5.193479
k	75.00000	78.25000	1	I	5.193479
l	74.00000	77.25000	1	I	5.193479

`round(model$pvalue,2)`

	A	B	C	D	e	f	g	h	i	j	k
B	0.23										
C	0.55	0.51									
D	0.76	0.35	0.76								
e	0.35	0.91	0.58	0.45							
f	0.78	0.28	0.51	0.64	0.35						
g	0.12	0.40	0.22	0.16	0.56	0.16					
h	0.21	0.06	0.12	0.16	0.11	0.38	0.05				
i	0.29	0.79	0.48	0.38	0.90	0.30	0.64	0.10			
j	0.45	0.94	0.71	0.57	0.88	0.38	0.48	0.11	0.79		
k	0.35	0.91	0.58	0.45	1.00	0.35	0.52	0.11	0.91	0.88	
l	0.29	0.79	0.48	0.38	0.91	0.30	0.61	0.10	1.00	0.79	0.90

## 4.12 NON-PARAMETRIC COMPARISONS

The functions for non-parametric multiple comparisons included in 'agricolae' are: `kruskal()`, `waerden.test()`, `friedman()` and `durbin.test()` (Conover, 1999).

The function `kruskal()` is used for N samples ( $N > 2$ ), populations or data coming from a completely random experiment (populations = treatments).

The function `waerden.test()`, similar to `kruskal-wallis`, uses a normal score instead of ranges as `kruskal` does.

The function `friedman()` is used for organoleptic evaluations of different products, made by judges (every judge evaluates all the products). It can also be used for the analysis of treatments of the randomized complete block design, where the response cannot be treated through the analysis of variance.

The function `durbin.test()` for the analysis of balanced incomplete block designs is very used for sampling tests, where the judges only evaluate a part of the treatments.

Montgomery book data (Montgomery, 2002)  
Included in the 'agricolae' package

```
library(agricolae)
data(corn)
attach(corn)
str(corn)
```

```
'data.frame': 34 obs. of 3 variables:
 $ method      : int  1 1 1 1 1 1 1 1 1 2 ...
 $ observation: int  83 91 94 89 89 96 91 92 90 91 ...
 $ rx          : num  11 23 28.5 17 17 31.5 23 26 19.5 23 ...
```

For the examples, the 'agricolae' package data will be used.

## 4.13 KRUSKAL-WALLIS

```
compare<-kruskal(observation,method,group=TRUE, main="corn")
```

```
Study: corn
Kruskal-Wallis test's
Ties or no Ties
```

```
Value: 25.62884
degrees of freedom: 3
Pvalue chisq : 1.140573e-05
```

```
method, means of the ranks
```

	observation	replication
1	21.83333	9
2	15.30000	10
3	29.57143	7
4	4.81250	8

```
t-Student: 2.042272
```

```
Alpha      : 0.05
LSD        : 4.9175
```

Harmonic Mean of Cell Sizes 8.351284  
Means with the same letter are not significantly different

Groups, Treatments and mean of the ranks

a	3	29.57
b	1	21.83
c	2	15.3
d	4	4.812

The object “compares” has the same structure of the comparisons (figure 4.3).

```
par(mfrow=c(1,2),cex=0.8,mar=c(3,3,1,0))
bar.group(compare,ylim=c(0,35),col=colors()[45])
bar.err(compare,ylim=c(0,35),col=colors()[25],std=F,
main="Std.Error")
```

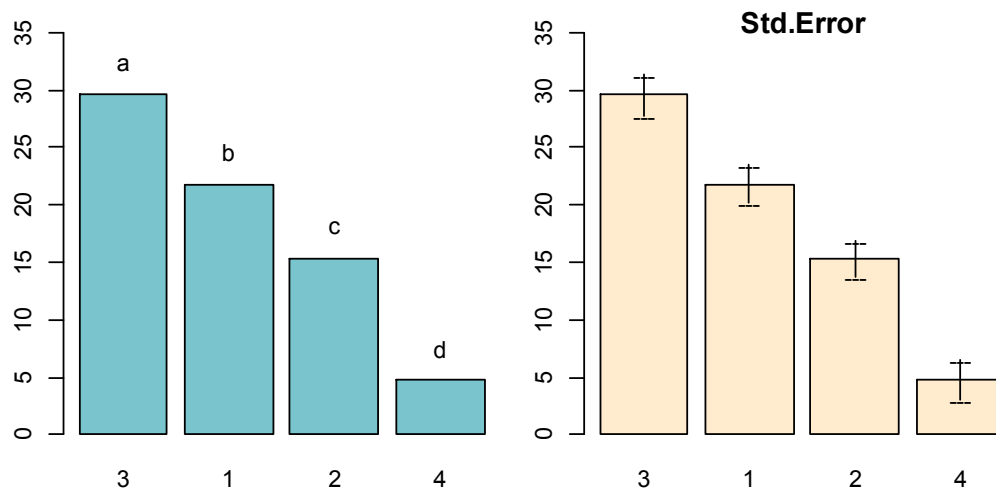


Figure 4.5. Comparison according to Waller-Duncan.

#### 4.14 FRIEDMAN

```
friedman()

rm(list=ls())
library(agricolae)
data(grass)
attach(grass)
compare<-friedman(judge,trt, evaluation,alpha=0.05, group=FALSE,
main="Data of the book of Conover")
```

Study: Data of the book of Conover

trt, Sum of the ranks

	evaluation	replication
t1	38.0	12
t2	23.5	12
t3	24.5	12
t4	34.0	12

Friedman's Test  
=====

Adjusted for ties  
Value: 8.097345  
Pvalue chisq : 0.04404214  
F value : 3.192198  
Pvalue F: 0.03621547

Alpha : 0.05  
t-Student : 2.034515

Comparison between treatments  
Sum of the ranks

	Difference	pvalue	sig	LCL	UCL
t1 - t2	14.5	0.014896	*	3.02	25.98
t1 - t3	13.5	0.022602	*	2.02	24.98
t1 - t4	4.0	0.483434		-7.48	15.48
t2 - t3	-1.0	0.860438		-12.48	10.48
t2 - t4	-10.5	0.071736	.	-21.98	0.98
t3 - t4	-9.5	0.101742		-20.98	1.98

#### 4.15 WAERDEN

waerden.test(), with the sweet potato data in the 'agricolae' basis.

```
data(sweetpotato)
attach(sweetpotato)
compare<-waerden.test(yield,virus,alpha=0.01,group=TRUE)
```

Study:  
Van der Waerden (Normal Scores) test's

Value : 8.409979  
Pvalue: 0.03825667  
Degrees of freedom: 3

virus, means of the normal score

	yield	replication
cc	-0.2328353	3
fc	-1.0601764	3
ff	0.6885684	3
oo	0.6044433	3

t-Student: 3.355387  
Alpha : 0.01  
LSD : 1.322487

Means with the same letter are not significantly different

```

Groups, Treatments and means of the normal score
a      ff      0.6886
a      oo      0.6044
ab     cc      -0.2328
b      fc      -1.06

```

The comparison probabilities are obtained with the parameter group=FALSE.

```

compare<-waerden.test(yield,virus,group=F)
detach(sweetpotato)

```

```

Study:
Van der Waerden (Normal Scores) test's

```

```

Value : 8.409979
Pvalue: 0.03825667
Degrees of freedom: 3

```

```

virus, means of the normal score

```

```

      yield replication
cc -0.2328353      3
fc -1.0601764      3
ff  0.6885684      3
oo  0.6044433      3

```

```

Comparison between treatments means
mean of the normal score

```

	Difference	pvalue	sig	LCL	UCL
cc - fc	0.8273411	0.069032	.	-0.08154345	1.73622564
cc - ff	-0.9214037	0.047582	*	-1.83028827	-0.01251917
cc - oo	-0.8372786	0.066376	.	-1.74616316	0.07160593
fc - ff	-1.7487448	0.002176	**	-2.65762936	-0.83986026
fc - oo	-1.6646197	0.002902	**	-2.57350426	-0.75573516
ff - oo	0.0841251	0.836322		-0.82475944	0.99300965

#### 4.16 DURBIN

durbin(); example: Myles Hollander (p. 311) Source: W. Moore and C.I. Bliss. (1942)

```

days <-gl(7,3)
chemical<-c("A","B","D","A","C","E","C","D","G","A","F","G",
"B","C","F","B","E","G","D","E","F")
toxic<-c(0.465,0.343,0.396,0.602,0.873,0.634,0.875,0.325,0.330,
0.423,0.987,0.426,0.652,1.142,0.989,0.536,0.409,0.309,
0.609,0.417,0.931)

```

```

compare<-durbin.test(days,chemical,toxic,group=F,
main="Logarithm of the toxic dose")

```

```

Study: Logarithm of the toxic dose
chemical, Sum of ranks

```

```

sum
A    5
B    5
C    9
D    5
E    5
F    8
G    5

```

```

Durbin Test
=====
Value      : 7.714286
Df 1       : 6
P-value    : 0.2597916
Alpha      : 0.05
Df 2       : 8
t-Student  : 2.306004

```

```

Least Significant Difference
between the sum of ranks:  5.00689

```

```

Parameters BIB
Lambda      : 1
treatmeans  : 7
Block size  : 3
Blocks      : 7
Replication : 3

```

```

Comparison between treatments sum of the ranks

```

	Difference	pvalue	sig
A - B	0	1.000000	
A - C	-4	0.102688	
A - D	0	1.000000	
A - E	0	1.000000	
A - F	-3	0.204420	
A - G	0	1.000000	
....			
E - F	-3	0.204420	
E - G	0	1.000000	
F - G	3	0.204420	

## 5 STABILITY ANALYSIS

In 'agricolae' there are two methods for the study of stability and the AMMI model. These are: a parametric model for a simultaneous selection in yield and stability "SHUKLA'S STABILITY VARIANCE AND KANG'S", and a non-parametric method of Haynes, based on the data range.

### 5.1 PARAMETRIC STABILITY

Use the parametric model, function `stability.par()`.

Prepare a data table where the rows and the columns are the genotypes and the environments, respectively. The data should correspond to yield averages or to another measured variable. Determine the variance of the common error for all the



environments and the number of repetitions that was evaluated for every genotype. If the repetitions are different, find a harmonious average that will represent the set. Finally, assign a name to each row that will represent the genotype. We will consider five environments in the following example:

```
v1 <- c(10.2, 8.8, 8.8, 9.3, 9.6, 7.2, 8.4, 9.6, 7.9, 10, 9.3, 8.0, 10.1, 9.4, 10.8, 6.3, 7.4)
v2 <- c(7, 7.8, 7.0, 6.9, 7, 8.3, 7.4, 6.5, 6.8, 7.9, 7.3, 6.8, 8.1, 7.1, 7.1, 6.4, 4.1)
v3 <- c(5.3, 4.4, 5.3, 4.4, 5.5, 4.6, 6.2, 6.0, 6.5, 5.3, 5.7, 4.4, 4.2, 5.6, 5.8, 3.9, 3.8)
v4 <- c(7.8, 5.9, 7.3, 5.9, 7.8, 6.3, 7.9, 7.5, 7.6, 5.4, 5.6, 7.8, 6.5, 8.1, 7.5, 5.0, 5.4)
v5 <- c(9, 9.2, 8.8, 10.6, 8.3, 9.3, 9.6, 8.8, 7.9, 9.1, 7.7, 9.5, 9.4, 9.4, 10.3, 8.8, 8.7)
```

For 17 genotypes, the identification is made by letters.

```
study <- data.frame(v1, v2, v3, v4, v5)
rownames(study) <- LETTERS[1:17]
```

An error variance of 2 and 4 repetitions is assumed.

```
stability <- stability.par(study, rep=4, MSError=2)
```

INTERACTIVE PROGRAM FOR CALCULATING SHUKLA'S STABILITY VARIANCE AND KANG'S

YIELD - STABILITY (YSi) STATISTICS

Environmental index - covariate

Analysis of Variance

	d.f.	Sum of Squares	Mean Squares	F	p.value
TOTAL	84	1035.6075			
GENOTYPES	16	120.0875	7.5055	2.65	0.003
ENVIRONMENTS	4	734.2475	183.5619	91.78	<0.001
INTERACTION	64	181.2725	2.8324	1.42	0.033
HETEROGENEITY	16	52.7128	3.2945	1.23	0.281
RESIDUAL	48	128.5597	2.6783	1.34	0.0815
POOLED ERROR	240		2		

Genotype. Stability statistics

	Mean	Sigma-square	. s-square	. Ecovalence
A	7.86	1.671833	ns 2.209084	ns 6.567031
B	7.22	1.822233	ns 1.977299	ns 7.097855
C	7.44	0.233967	ns 0.134103	ns 1.492208
D	7.42	4.079567	ns 1.443859	ns 15.064913
E	7.64	2.037967	ns 2.369090	ns 7.859266
F	7.14	5.161967	* 6.763106	* 18.885149
G	7.90	1.759300	ns 1.058092	ns 6.875737
H	7.68	1.757167	ns 2.028880	ns 6.868208
I	7.34	5.495300	* 0.423680	ns 20.061619
J	7.54	4.129967	ns 5.125514	ns 15.242796
K	7.12	3.848900	ns 4.360772	ns 14.250796
L	7.30	2.675300	ns 3.610982	ns 10.108678
M	7.66	3.473167	ns 2.198229	ns 12.924678
N	7.92	0.806233	ns 1.097156	ns 3.511972
O	8.30	1.951300	ns 1.459578	ns 7.553384
P	6.08	3.647833	ns 4.919102	ns 13.541149
Q	5.88	3.598500	ns 4.353030	ns 13.367031

Signif. codes: 0 '\*\*\*' 0.01 '\*\*' 0.05 'ns' 1

Simultaneous selection for yield and stability (++)

	Yield	Rank	Adj.rank	Adjusted	Stab.var	Stab.rating	YSi	...
A	7.86	14	1	15	1.671833	0	15	+
B	7.22	5	-1	4	1.822233	0	4	
C	7.44	9	1	10	0.233967	0	10	+
D	7.42	8	1	9	4.079567	-2	7	
E	7.64	11	1	12	2.037967	0	12	+
F	7.14	4	-1	3	5.161967	-4	-1	
G	7.90	15	1	16	1.759300	0	16	+
H	7.68	13	1	14	1.757167	0	14	+
I	7.34	7	-1	6	5.495300	-4	2	
J	7.54	10	1	11	4.129967	-2	9	+
K	7.12	3	-1	2	3.848900	0	2	
L	7.30	6	-1	5	2.675300	0	5	
M	7.66	12	1	13	3.473167	0	13	+
N	7.92	16	1	17	0.806233	0	17	+
O	8.30	17	2	19	1.951300	0	19	+
P	6.08	2	-2	0	3.647833	0	0	
Q	5.88	1	-3	-2	3.598500	0	-2	

Yield Mean: 7.378824

YS Mean: 8.352941

LSD (0.05): 0.7384513

- - - - -

+ selected genotype

++ Reference: Kang, M. S. 1993. Simultaneous selection for yield and stability: Consequences for growers. Agron. J. 85:754-757.

The selected genotypes are: A, C, E, G, H, J, M, N and O. These genotypes have a higher yield and a lower variation. According to the ANOVA, the interaction is significant.

If for example there is an environmental index, it can be added as a covariate. For this case, the altitude of the localities is included.

```
altitude<-c(1200, 1300, 800, 1600, 2400)
stability <- stability.par(study,rep=4,MSerror=2, cova=TRUE,
name.cov= "altitude", file.cov= altitude)
```

## 5.2 NON-PARAMETRIC STABILITY

For non-parametric stability, the function in 'agricolae' is `stability.nonpar()`. The names of the genotypes should be included in the first column, and in the other columns, the response by environments.

```
data <- data.frame(name=row.names(study), study)
model<-stability.nonpar(data, "YIELD", ranking=TRUE)
```

Nonparametric Method for Stability Analysis

-----

Estimation and test of nonparametric measures

Variable: YIELD

Ranking...

	v1	v2	v3	v4	v5
A	16.0	8.0	9	14.0	8.0
B	7.5	14.0	5	5.5	10.0
C	7.5	8.0	9	9.0	6.0
D	9.5	6.0	5	5.5	17.0
E	12.5	8.0	11	14.0	3.0
F	2.0	17.0	7	7.0	11.0
G	6.0	13.0	16	16.0	15.0
H	12.5	3.0	15	10.5	6.0
I	4.0	4.5	17	12.0	2.0
J	14.0	15.0	9	2.5	9.0
K	9.5	12.0	13	4.0	1.0
L	5.0	4.5	5	14.0	14.0
M	15.0	16.0	3	8.0	12.5
N	11.0	10.5	12	17.0	12.5
O	17.0	10.5	14	10.5	16.0
P	1.0	2.0	2	1.0	6.0
Q	3.0	1.0	1	2.5	4.0

Statistics...

	Mean	Rank	s1	Z1	s2	Z2
A	7.86	14	5.4	0.02	21.5	0.04
B	7.22	5	6.2	0.12	25.7	0.02
C	7.44	9	3.0	2.73	7.5	1.83
D	7.42	8	7.4	1.20	36.5	1.05
E	7.64	11	5.6	0.00	21.8	0.03
F	7.14	4	7.8	1.81	39.2	1.55
G	7.90	15	5.2	0.08	18.7	0.19
H	7.68	13	6.2	0.12	25.3	0.01
I	7.34	7	8.8	3.87	51.5	5.08
J	7.54	10	7.2	0.94	34.3	0.71
K	7.12	3	7.8	1.81	43.0	2.43
L	7.30	6	7.4	1.20	34.7	0.77
M	7.66	12	7.6	1.49	38.2	1.36
N	7.92	16	4.2	0.82	14.8	0.57
O	8.30	17	7.0	0.71	31.7	0.40
P	6.08	2	6.6	0.35	27.7	0.09
Q	5.88	1	7.0	0.71	32.3	0.46

Sum of Z1: 17.97158

Sum of Z2: 16.59462

Test...

The Z-statistics are measures of stability. The test for the significance of the sum of Z1 or Z2 are compared to a Chi-Square value of chi.sum. individual Z1 or Z2 are compared to a Chi-square value of chi.ind.

	MEAN	es1	es2	vs1	vs2	chi.ind	chi.sum
1	7.378824	5.647059	24	2.566667	148.8	8.843605	27.58711

---

expectation and variance: es1, es2, vs1, vs2

### 5.3 AMMI

The model AMMI uses the biplot constructed through the principal components generated by the interaction environment-genotype. If there is such interaction, the percentage of the two principal components would explain more than the 50% of the total variation; in such case, the biplot would be a good alternative to study the interaction environment-genotype.

The data for AMMI should come from similar experiments conducted in different environments. Homogeneity of variance of the experimental error, produced in the different environments, is required. The analysis is done by combining the experiments.

The data can be organized in columns, thus: environment, genotype, repetition, and variable.

The data can also be the averages of the genotypes in each environment, but it is necessary to consider a harmonious average for the repetitions and a common variance of the error. The data should be organized in columns: environment, genotype, and variable.

When performing AMMI, this generates the BIPLLOT graphics; see figure 5.1.

For the application, we consider the data used in the example of parametric stability (study):

```
par(mar=c(4,4,0,0))
rdto <- c(study[,1], study[,2], study[,3], study[,4], study[,5])
environment <- gl(5,17)
genotype <- rep(rownames(study),5)
model<-AMMI(ENV=environment, GEN=genotype, REP=4, Y=rdto, MSE=2,
ylim=c(-2,2), xlim=c(-2,2), number=FALSE)
```

```
ANALYSIS AMMI: rdto
Class level information
```

```
ENV:  1 2 3 4 5
GEN:  A B C D E F G H I J K L M N O P Q
REP:  4
```

```
Number of means:  85
```

```
Dependent Variable: rdto
```

```
Analysis of variance
```

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
ENV	4	734.2475	183.561882		
REP(ENV)	15				
GEN	16	120.0875	7.505471	3.752735	3.406054e-06
ENV:GEN	64	181.2725	2.832382	1.416191	3.279630e-02
Residuals	240	480.0000	2.000000		

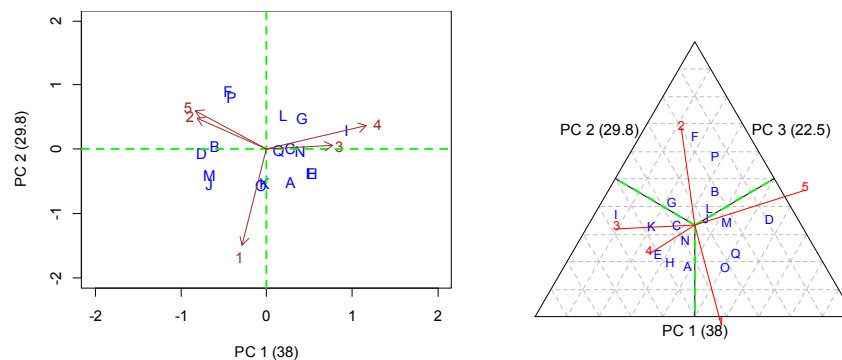
```
Coeff var      Mean rdto
19.16584       7.378824
```

```

Analysis
percent acum Df Sum.Sq Mean.Sq F.value Pr.F
PC1 38.0 38.0 19 68.96258 3.629609 1.81 0.0225
PC2 29.8 67.8 17 54.02864 3.178155 1.59 0.0675
PC3 22.5 90.3 15 40.84756 2.723170 1.36 0.1680
PC4 9.6 99.9 13 17.43370 1.341054 0.67 0.7915
PC5 0.0 99.9 11 0.00000 0.000000 0.00 1.0000

require(klaR)
par(mar=c(4,4,0,0))
model<-AMMI (ENV=environment, GEN=genotype, REP=4, Y=rdto, MSE=2,
graph="triplot",number=F)

```



**Figure 5.1. Biplot and Triplot**

In this case, the interaction is significant. The first two components explain 67.8%; then the biplot can provide information about the interaction genotype-environment. With the triplot, 90.3% would be explained.

## 6 SPECIAL FUNCTIONS

### 6.1 CONSENSUS OF DENDROGRAM

Consensus is the degree or similarity of the vertexes of a tree regarding its branches of the constructed dendrogram. The function to apply is `consensus()`.

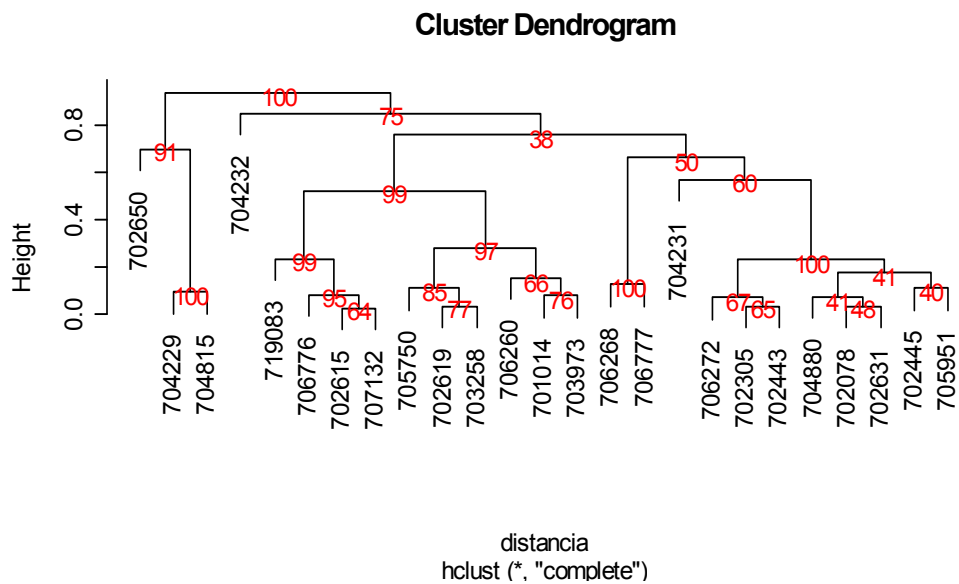
The data correspond to a table, with the name of the individuals and the variables in the rows and columns respectively. For the demonstration, we will use the “pamCIP” data of ‘agricolae’, which correspond to molecular markers of 43 entries of a germplasm bank (rows) and 107 markers (columns).

The program identifies duplicates in the rows and can operate in both cases. The result is a dendrogram, in which the consensus percentage is included, figure 6.1.

```

data (pamCIP)
rownames (pamCIP) <- substr (rownames (pamCIP), 1, 6)
par (cex=0.8)
output<-consensus (pamCIP,distance="binary", method="complete",
nboot=500)

```



**Figure 6.1. Dendrogram, production by consensus()**

Duplicates: 18

New data : 25 Records

Consensus hclust

Method distance: binary

Method cluster : complete

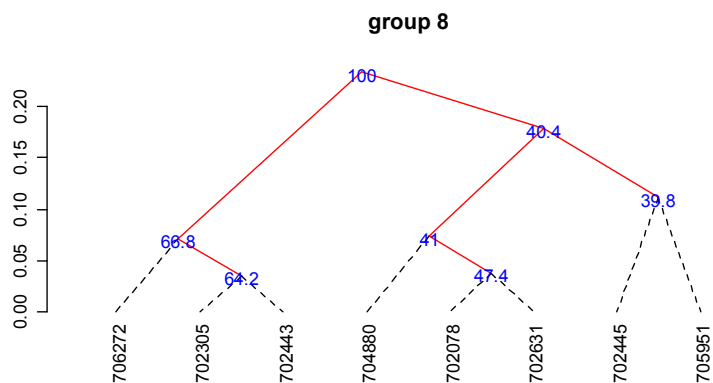
rows and cols : 25 107

n-bootstrap : 500

Run time : 20.469 secs

When the dendrogram is complex, it is convenient to extract part of it with the function `hcut()`, figure 6.2.

```
hcut(output,h=0.4,group=8,type="t",edgePar = list(lty=1:2,
col=2:1),main="group 8" ,col.text="blue",cex.text=1)
```



**Figure 6.2. Dendrogram, production by hcut()**

The obtained object "output" contains information about the process:

```
names(output)

[1] "table.dend" "dendrogram" "duplicates"
```

This means that we can know the duplicates, reconstruct the tree diagram and maintain the interactions.

```
output$table.dend
```

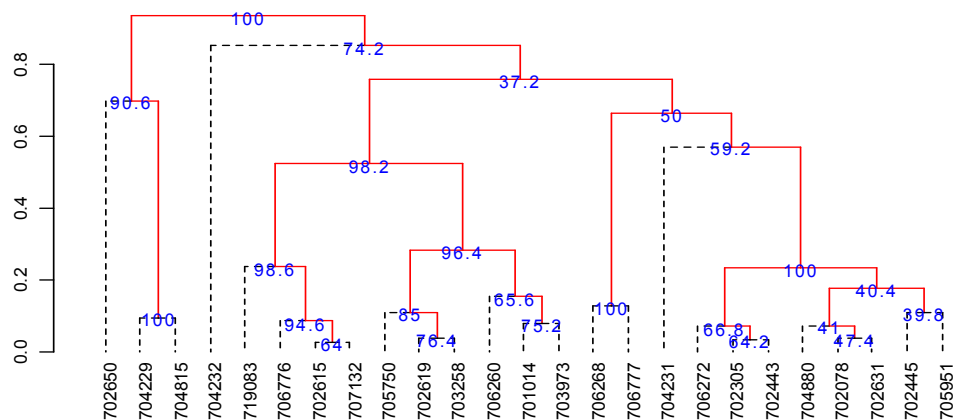
	X1	X2	axis	height	percentage	groups
1	-6	-24	7.500000	0.02857143	64.0	6-24
2	-3	-4	19.500000	0.03571429	64.2	3-4
...						
24	21	23	5.099609	0.93617021	100.0	1-2-3-4-5-6-7-8-9-10-11-
	12-13-14-15-16-17-18-19-20-21-22-23-24-25					

Reproduce the dendrogram:

```
dend<-output$dendrogram
data<-output$table.dend
plot(dend)
text(data[,3],data[,4],data[,5])
```

Construct a classic dendrogram, figure 6.3

```
dend<-as.dendrogram(output$dendrogram)
plot(dend,type="r",edgePar = list(lty=1:2, col=2:1))
text(data[,3],data[,4],data[,5],col="blue",cex=1)
```



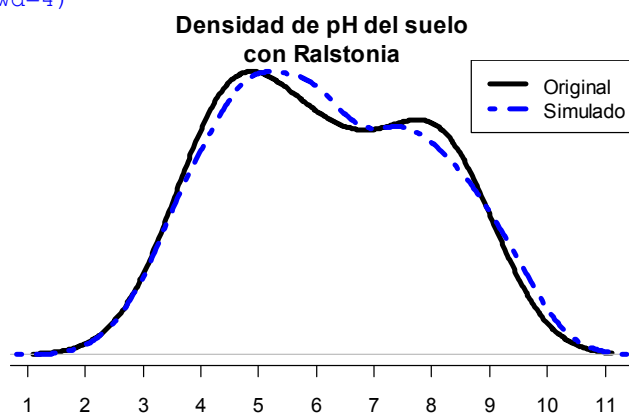
**Figure 6.3. Classic dendrogram**

## 6.2 MONTECARLO

It is a method for generating random numbers of an unknown distribution. It uses a data set and, through the cumulative behavior of its relative frequency, generates the possible random values that follow the data distribution. These new numbers are used in some simulation process.

The probability density of the original and simulated data can be compared, figure 6.4.

```
data(soil)
set.seed(9473)
simulated <- montecarlo(soil$pH,1000)
par(mar=c(3,0,2,1))
plot(density(soil$pH),axes=F,main="pH density of the soil\ncon
Ralstonia",xlab="",lwd=4)
lines(density(simulated), col="blue", lty=4,lwd=4)
h<-graph.freq(simulated,plot=F)
axis(1,0:12)
legend("topright",c("Original","Simulated"),lty=c(1,4),col=c("black"
, "blue"), lwd=4)
```



**Figure 6.4. Distribution of the simulated and the original data**

1000 data have been generated, being the frequency table:

```
round(table.freq(h),2)
```

Lower	Upper	Main	freq	relative	CF	RCF
2.00	2.79	2.40	12	0.01	12	0.01
2.79	3.58	3.19	50	0.05	62	0.06
. . . .						
9.11	9.90	9.51	49	0.05	989	0.99
9.90	10.69	10.30	11	0.01	1000	1.00

Some statistics:

```
summary(soil$pH)
```

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
3.800	4.700	6.100	6.154	7.600	8.400

```
summary(simulated)
```

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
1.443	4.698	6.022	6.209	7.762	10.950



### 6.3 RE-SAMPLING IN LINEAR MODEL

It uses the permutation method for the calculation of the probabilities of the sources of variation of ANOVA according to the linear regression model or the design used. The principle is that the Y response does not depend on the averages proposed in the model; hence, the Y values can be permuted and many model estimates can be constructed. On the basis of the patterns of the random variables of the elements under study, the probability is calculated in order to measure the significance.

For a variance analysis, the data should be prepared similarly. The function to use is: `resampling.model()`

```
data(potato)
potato[,1]<-as.factor(potato[,1])
potato[,2]<-as.factor(potato[,2])
model<-"cutting~variety + date + variety:date"
analysis<-resampling.model(model, potato, k=1000)
```

Resampling of the experiments

-----

Proposed model: cutting~variety + date + variety:date

---

Resampling of the analysis of variance for the proposed model

Determination of the P-Value by Resampling

Samples: 1000

	Df	Sum Sq	Mean Sq	F value	Pr(>F)	Resampling
variety	1	25.086806	25.086806	7.2580377	0.01952218	0.025
date	2	13.891758	6.945879	2.0095604	0.17670768	0.200
variety:date	2	4.853025	2.426513	0.7020312	0.51483592	0.530
Residuals	12	41.477005	3.456417			

---

The function `resampling.model()` can be used when the errors have a different distribution from normal.

### 6.4 SIMULATION IN LINEAR MODEL

Under the assumption of normality, the function generates pseudo experimental errors under the proposed model, and determines the proportion of valid results according to the analysis of variance found.

The function is: `simulation.model()`. The data are prepared in a table, similarly to an analysis of variance.

Considering the example proposed in the previous procedure:

```
model <- simulation.model(model, potato, k=1000)
```

Simulation of experiments

Under the normality assumption

-----

Proposed model: cutting~variety + date + variety:date

Analysis of Variance Table

```

Response: cutting
      Df Sum Sq Mean Sq F value    Pr(>F)
variety  1 25.087   25.087    7.2580 0.01952 *
date     2 13.892    6.946    2.0096 0.17671
variety:date  2  4.853    2.427    0.7020 0.51484
Residuals 12 41.477    3.456
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
---
Validation of the analysis of variance for the proposed model
Simulations: 1000

```

```

      Df    F value % Acceptance % Rejection Criterion
variety  1 7.2580377         51.5         48.5 acceptable
date     2 2.0095604         61.1         38.9 acceptable
variety:date  2 0.7020312         67.5         32.5 acceptable
---

```

The validation is referred to the percentage of decision results equal to the result of the ANOVA decision. Thus, 67.5% of the results simulated on the interaction variety\*date gave the same result of acceptance or rejection obtained in the ANOVA.

## 6.5 PATH ANALYSIS

It corresponds to the “path analysis” method. The data correspond to correlation matrices of the independent ones with the dependent matrix (XY) and between the independent ones (XX).

It is necessary to assign names to the rows and columns in order to identify the direct and indirect effects.

```

corr.x<- matrix(c(1,0.5,0.5,1),c(2,2))
corr.y<- rbind(0.6,0.7)
names<-c("X1","X2")
dimnames(corr.x)<-list(names,names)
dimnames(corr.y)<-list(names,"Y")
output<-path.analysis(corr.x,corr.y)

```

Direct(Diagonal) and indirect effect path coefficients

```

=====
              X1              X2
X1 0.3333333 0.2666667
X2 0.1666667 0.5333333

```

Residual Effect^2 = 0.4266667

```

> output
$Coeff
              X1              X2
X1 0.3333333 0.2666667
X2 0.1666667 0.5333333

$Residual
[1] 0.4266667

```

## 6.6 LINE X TESTER

It corresponds to a crossbreeding analysis of a genetic design. The data should be organized in a table. Only four columns are required: repetition, females, males, and response. In case it corresponds to progenitors, the females or males field will only be filled with the corresponding one. See the heterosis data.

Example with the heterosis data, locality 2.

	Replication	Female	Male	v2
109	1	LT-8	TS-15	2.65
110	1	LT-8	TPS-13	2.26
...				
131	1	Achirana	TPS-13	3.55
132	1	Achirana	TPS-67	3.05
133	1	LT-8	<NA>	2.93
134	1	TPS-2	<NA>	2.91
...				
140	1	Achirana	<NA>	3.35
...				
215	3	<NA>	TPS-67	2.91

where <NA> is empty.

If it is a progeny, it comes from a "Female" and a "Male."  
If it is a progenitor, it will only be "Female" or "Male."

The following example corresponds to data of the locality 2:

24 progenies  
8 females  
3 males  
3 repetitions

They are 35 treatments (24, 8, 3) applied to three blocks.

```
data(heterosis)
site2<-subset(heterosis,heterosis[,1]==2)
site2<-subset(site2[,c(2,5,6,8)],site2[,4]!="Control")
attach(site2)
output1<-lineXtester(Replication, Female, Male, v2)
detach(site2)
```

ANALYSIS LINE x TESTER: v2

ANOVA with parents and crosses

```
=====
```

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Replications	2	0.519190476	0.259595238	9.801	0.0002
Treatments	34	16.101605714	0.473576639	17.879	0.0000
Parents	10	7.731490909	0.773149091	29.189	0.0000
Parents vs. Crosses	1	0.005082861	0.005082861	0.192	0.6626
Crosses	23	8.365031944	0.363697041	13.731	0.0000
Error	68	1.801142857	0.026487395		
Total	104	18.421939048			

# ANOVA for line X tester analysis

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Lines	7	4.9755431	0.71079187	3.632	0.0191
Testers	2	0.6493861	0.32469306	1.659	0.2256
Lines X Testers	14	2.7401028	0.19572163	7.389	0.0000
Error	68	1.8011429	0.02648739		

# ANOVA for line X tester analysis including parents

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Replications	2	0.519190476	0.259595238	9.801	0.0002
Treatments	34	16.101605714	0.473576639	17.879	0.0000
Parents	10	7.731490909	0.773149091	29.189	0.0000
Parents vs. Crosses	1	0.005082861	0.005082861	0.192	0.6626
Crosses	23	8.365031944	0.363697041	13.731	0.0000
Lines	7	4.975543056	0.710791865	3.632	0.0191
Testers	2	0.649386111	0.324693056	1.659	0.2256
Lines X Testers	14	2.740102778	0.195721627	7.389	0.0000
Error	68	1.801142857	0.026487395		
Total	104	18.421939048			

## GCA Effects:

=====

## Lines Effects:

Achirana	LT-8	MF-I	MF-II	Serrana	TPS-2	TPS-25	TPS-7
0.022	-0.338	0.199	-0.449	0.058	-0.047	0.414	0.141

## Testers Effects:

TPS-13	TPS-67	TS-15
0.087	0.046	-0.132

## SCA Effects:

=====

	Testers		
Lines	TPS-13	TPS-67	TS-15
Achirana	0.061	0.059	-0.120
LT-8	-0.435	0.519	-0.083
MF-I	-0.122	-0.065	0.187
MF-II	-0.194	0.047	0.148
Serrana	0.032	-0.113	0.081
TPS-2	0.197	-0.072	-0.124
TPS-25	0.126	-0.200	0.074
TPS-7	0.336	-0.173	-0.162

## Standard Errors for Combining Ability Effects:

=====

S.E. (gca for line)	: 0.05424983
S.E. (gca for tester)	: 0.0332211
S.E. (sca effect)	: 0.09396346
S.E. (gi - gj)line	: 0.07672084
S.E. (gi - gj)tester	: 0.04698173
S.E. (sij - skl)tester	: 0.1328844

## Genetic Components:

=====

Cov H.S. (line)	: 0.05723003
Cov H.S. (tester)	: 0.00537381

```

Cov H.S. (average): 0.003867302
Cov F.S. (average): 0.1279716

F = 0, Additive genetic variance: 0.01546921
F = 1, Additive genetic variance: 0.007734604
F = 0, Variance due to Dominance: 0.1128228
F = 1, Variance due to Dominance: 0.05641141

Proportional contribution of lines, testers
and their interactions to total variance
=====
Contributions of lines : 59.48026
Contributions of testers: 7.763104
Contributions of lxt : 32.75663

```

## 6.7 SOIL UNIFORMITY

The Smith index is an indicator of the uniformity, used to determine the parcel size for research purposes. The data correspond to a matrix or table that contains the response per basic unit, a number of n rows x m columns, and a total of n\*m basic units.

For the test, we will use the rice file. The graphic is a result with the adjustment of a model for the parcel size and the coefficient of variation, figure 6.5.

```

data(rice)
table<-index.smith(rice,
  main="Interaction between the CV and the parcel size" ,col="red",
  type="l",xlab="Size")
uniformity <- data.frame(table$uniformity)

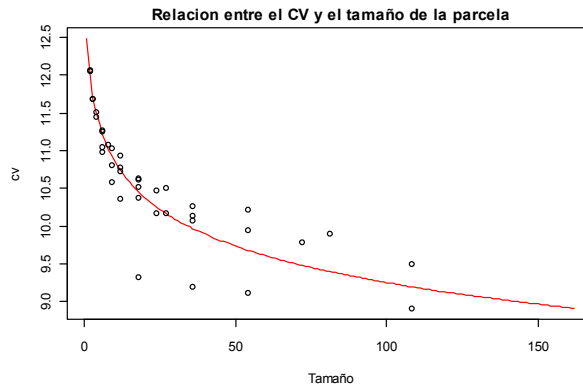
```

```

uniformity
  Size Width Length plots      Vx    CV
1     1     1      1    648 9044.539 13.0
2     2     1      2    324 7816.068 12.1
3     2     2      1    324 7831.232 12.1
4     3     1      3    216 7347.975 11.7
5     3     3      1    216 7355.216 11.7
...
40  162     9     18      4 4009.765  8.6

```

The size is the product of the width x the length of the parcel, and the rectangle size is the product of the width x the length.



**Figure 6.5. Adjustment curve for the optimal size of parcel**

## 6.8 CONFIDENCE LIMITS IN BIODIVERSITY INDICES

The biodiversity indices are widely used for measuring the presence of living things in an ecological area. Many programs indicate their value. The function of 'agricolae' is also to show the confidence intervals, which can be used for a statistical comparison. Use the bootstrap procedure. The data are organized in a table; the species are placed in a column; and in another one, the number of individuals. The indices that can be calculated with the function `index.bio()` of 'agricolae' are: "Margalef", "Simpson.Dom", "Simpson.Div", "Berger.Parker", "McIntosh", and "Shannon."

In the example below, we will use the data obtained in the locality of Paracsho, district of Huasahuasi, province of Tarma in the department of Junín.

The evaluation was carried out in the parcels on 17 November 2005, without insecticide application. The counted specimens were the following:

```
data(paracsho)
species <- paracsho[79:87,4:6]
species
```

	Order	Family	Number.of.specimens
79	DIPTERA	TIPULIDAE	3
80	LEPIDOPTERA	NOCTUIDAE	1
81	NOCTUIDAE	PYRALIDAE	3
82	HEMIPTERA	ANTHOCORIDAE	1
83	DIPTERA	TACHINIDAE	16
84	DIPTERA	ANTHOCORIDAE	3
85	DIPTERA	SCATOPHAGIDAE	5
86	DIPTERA	SYRPHIDAE	1
87	DIPTERA	MUSCIDAE	3

The Shannon index is:

```
output <- index.bio(species[,3],method="Shannon",level=95,nboot=200)
```

```
Method: Shannon  
Index: 3.52304
```

```
95 percent confidence interval:  
3.088775 ; 4.286088
```

## 6.9 CORRELATION

The function `correlation()` of 'agricolae' makes the correlations through the methods of Pearson, Spearman and Kendall for vectors and/or matrices. If they are two vectors, the test is carried out for one or two lines; if it is a matrix one, it determines the probabilities for a difference, whether it is greater or smaller.

For its application, consider the soil data: `data(soil)`

```
data(soil)  
correlation(soil[,2:4],method="pearson")
```

Correlation Analysis

```
Method      : pearson  
Alternative: two.sided
```

```
$correlation  
      pH    EC CaCO3  
pH    1.00 0.55 0.73  
EC     0.55 1.00 0.32  
CaCO3 0.73 0.32 1.00
```

```
$pvalue  
      pH          EC          CaCO3  
pH    1.000000000 0.0525330 0.004797027  
EC     0.052532997 1.0000000 0.294159813  
CaCO3 0.004797027 0.2941598 1.000000000
```

```
$n.obs  
[1] 13
```

```
attach(soil)  
correlation(pH,soil[,3:4],method="pearson")  
Correlation Analysis
```

```
Method      : pearson  
Alternative: two.sided
```

```
$correlation  
      EC CaCO3  
pH 0.55 0.73
```

```
$pvalue  
      EC CaCO3  
pH 0.0525 0.0048
```

```

$n.obs
[1] 13

correlation(pH,CaCO3,method="pearson")

Pearson's product-moment correlation

data: pH and CaCO3
t = 3.520169 , df = 11 , p-value = 0.004797027
alternative hypothesis: true rho is not equal to 0
sample estimates:
cor
0.7278362

```

## 6.10 OTHER FUNCTIONS

Desirability functions that facilitate the data management:

`tapply.stat()` Calculation of statesmen and mathematical operations in columns of a table in relation to grouped factors.

Factor and variable table

Application with 'agricolae' data:

```

data(RioChillon)
attach(RioChillon$babies)
tapply.stat(yield,farmer,function(x) max(x)-min(x))
detach(RioChillon$babies)

```

	farmer	yield
1	AugustoZambrano	7.5
2	Caballero	13.4
3	ChocasAlto	14.1
4	FelixAndia	19.4
5	Huarangal-1	9.8
6	Huarangal-2	9.1
7	Huarangal-3	9.4
8	Huatocay	19.4
9	IgnacioPolinario	13.1

It corresponds to the range of variation in the farmers' yield.

The function "tapply" can be used directly or with function.

If A is a table with columns 1,2 and 3 as factors, and 5,6 and 7 as variables, then the following procedures are valid:

```

tapply.stat(A[,5:7], A[,1:3],mean)
tapply.stat(A[,5:7], A[,1:3],function(x) mean(x,na.rm=TRUE))
tapply.stat(A[,c(7,6)], A[,1:2],function(x) sd(x)*100/mean(x))

```

### Coefficient of variation of an experiment

If "model" is the object resulting from an analysis of variance of the function `aov()` or `lm()` of R, then the function `cv.model()` calculates the coefficient of variation.



```
data(sweetpotato)
model <- model<-aov(yield ~ virus, data=sweetpotato)
cv.model(model)
[1] 17.16660
```

### Skewness and curtosis

The skewness and curtosis results, obtained by 'agricolae', are equal to the ones obtained by SAS, MiniTab, SPSS, InfoStat, and Excel.

If x represents a data set:

```
> x<-c(3,4,5,2,3,4,5,6,4,NA,7)
```

skewness is calculated with:

```
> skewness(x)
[1] 0.3595431
```

and curtosis with:

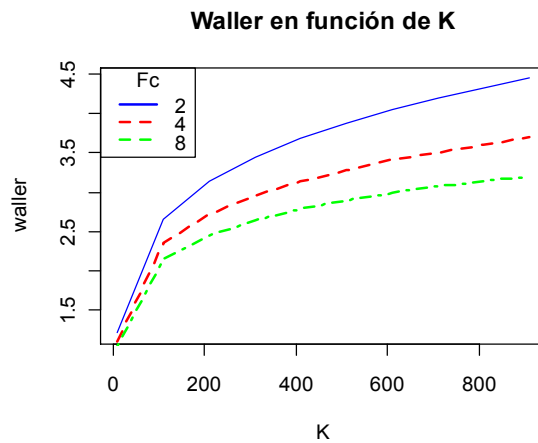
```
> kurtosis(x)
[1]-0.1517996
```

### Tabular value of Waller-Duncan

The function Waller determines the tabular value of Waller-Duncan. For the calculation, value F is necessary, calculated from the analysis of variance of the study factor, with its freedom degrees and the estimate of the variance of the experimental error. Value K, parameter of the function is the ratio between the two types of errors (I and II). To use it, a value associated with the alpha level is assigned. When the alpha level is 0.10, 50 is assigned to K; for 0.05, K=100; and for 0.01, K=500. K can take any value.

Figure 6.6 illustrates the function for different values of K with freedom degrees of 5 for the numerator and 15 for the denominator, and values of calculated F, equal to 2, 4, and 8.

```
q<-5
f<-15
K<-seq(10,1000,100)
n<-length(K)
y<-rep(0,3*n)
dim(y)<-c(n,3)
for(i in 1:n) y[i,1]<-waller(K[i],q,f,Fc=2)
for(i in 1:n) y[i,2]<-waller(K[i],q,f,Fc=4)
for(i in 1:n) y[i,3]<-waller(K[i],q,f,Fc=8)
plot(K,y[,1],type="l",col="blue",ylab="waller")
lines(K,y[,2],type="l",col="red",lty=2,lwd=2)
lines(K,y[,3],type="l",col="green",lty=4,lwd=2)
legend("topleft",c("2","4","8"),col=c("blue","red","green"),lty=c(1,
8,20),lwd=2,title="Fc")
title(main="Waller in function of K")
```

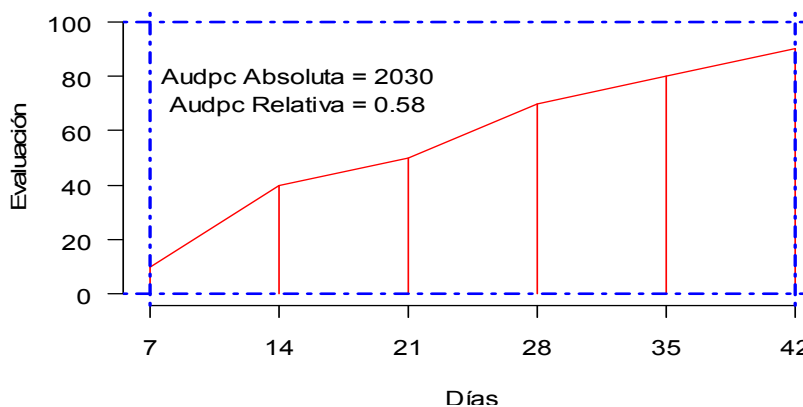


**Figure 6.6. Function of Waller to different value of parameters K and Fc**

## AUDPC

The area under the disease progress curve (AUDPC), (see figure 6.7), calculates the absolute and relative progress of the disease. It is required to measure the disease in percentage terms during several dates, preferably equidistantly.

```
days<-c(7,14,21,28,35,42)
evaluation<-data.frame(E1=10,E2=40,E3=50,E4=70,E5=80,E6=90)
plot(days,
evaluation,type="h",ylim=c(0,100),axes=F,col="red",xlab="Days",
ylab="Evaluation")
lines(days,evaluation,col="red")
axis(1,days)
axis(2,seq(0,100,20),las=2)
abline(v=7,h=100,lty=4,lwd=2,col="blue")
abline(v=42,h=0,lty=4,lwd=2,col="blue")
audpc(evaluation,days)
audpc(evaluation,days,"relative")
text(15,80,"Audpc Absolute = 2030")
text(15,70,"Audpc Relative = 0.58")
```



**Figure 6.7. AUDPC: Area under the curve**

## NON-ADDITIVITY

Tukey's test for non-additivity is used when there are doubts about the additivity veracity of a model. This test confirms such assumption and it is expected to accept the null hypothesis of the non-additive effect of the model.

For this test, all the experimental data used in the estimation of the linear additive model are required.

Use the function `nonadditivity()` of 'agricolae'. For its demonstration, the experimental data "potato", of the package 'agricolae', will be used. In this case, the model corresponds to the randomized complete block design, where the treatments are the varieties.

```
data(potato)
potato[,1]<-as.factor(potato[,1])
model<-lm(cutting ~ date + variety,potato)
df<-df.residual(model)
MSerror<-deviance(model)/df
attach(potato)
analysis<-nonadditivity(cutting, date, variety, df, MSerror)
detach(potato)
```

```
Tukey's test of non-additivity
cutting
```

```
P : 15.37166
Q : 77.4444
```

Analysis of Variance Table

Response: residual

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Non-additivity	1	3.051	3.051	0.922	0.3532
Residuals	14	46.330	3.309		

According to the results, the model is additive because the p.value 0.35 is greater than 0.05.

**Table 6.10. ASCII Character Code Reference for the use of symbols**

<b>ASCII Codes Table used in R</b>					
<b>Code</b>	<b>Symbol</b>	<b>Code</b>	<b>Symbol</b>	<b>Code</b>	<b>Symbol</b>
<b>92</b>	<b>}</b>	<b>124</b>	<b> </b>	<b>64</b>	<b>@</b>
<b>47</b>	<b>/</b>	<b>60</b>	<b>&lt;</b>	<b>94</b>	<b>^</b>
<b>91</b>	<b>[</b>	<b>62</b>	<b>&gt;</b>	<b>35</b>	<b>#</b>
<b>93</b>	<b>]</b>	<b>61</b>	<b>=</b>	<b>36</b>	<b>\$</b>
<b>40</b>	<b>(</b>	<b>34</b>	<b>"</b>	<b>37</b>	<b>%</b>
<b>41</b>	<b>)</b>	<b>126</b>	<b>~</b>	<b>38</b>	<b>&amp;</b>
<b>123</b>	<b>{</b>	<b>58</b>	<b>:</b>	<b>39</b>	<b>'</b>
<b>125</b>	<b>}</b>	<b>59</b>	<b>;</b>		

## **REFERENCES**

1. Cochran and Cox. (1992). Experimental Design. Second edition. Wiley Classics Library Edition published. John Wiley & Sons, INC.
2. Conover, W.J. (1999). Practical Nonparametrics Statistics. John Wiley & Sons, INC, New York.
3. De Mendiburu, Felipe (2009). Una herramienta de análisis estadístico para la investigación agrícola. Tesis. Universidad Nacional de Ingeniería (UNI).
4. Joshi, D.D. (1987). Linear Estimation and Design of Experiments. WILEY EASTERN LIMITED, New Delhi, India.
5. Kang, M. S. (1993). Simultaneous Selection for Yield and Stability: Consequences for Growers. Agron. J. 85:754-757.
6. Kuehl, Robert (2000). Design of Experiments. 2nd ed., Duxbury.
7. LeClerg, Erwin (1962). Field Plot Technique, Burgess Publishing Company.
8. Montgomery (2002). Diseño y Análisis de Experimentos (2ª Ed) WILEY.
9. Patterson, H.D. and Williams, E.R. Biometrika (1976). A New Class of Resolvable Incomplete Block Designs. Printed in Great Britain.
10. R Development Core Team (2012). R: A language and environment for statistical computing. R Foundation for Statistical Computing, Vienna, Austria. ISBN 3-900051-07-0, URL <http://www.R-project.org>.
11. Steel & Torry & Dickey (1997). Principles and Procedures of Statistics. A Biometrical Approach. Third Edition.